Version 2.0

System Documentation

LOLA – Library of Location Algorithms¹

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Chapter 1

Introduction

Finding "good" locations for facilities becomes more and more important in modern industry. The selection of optimized sites is essential for the efficient realization of technical methods. Examples can be found in microelectronics, the location of machines in industrial plants, the location of warehouses or depots, the location of emergency facilities or of undesireable facilities such as incinerators, etc.

The software library LOLA is designed to solve location problems and to suggest an optimized site for the specified problem. LOLA provides a graphical user interface that allows its simple application in industrial projects as well as for demonstrations in high school and university teaching. Furthermore a programming interface allows the use of the program library of LOLA for the implementation of extended routines to solve individual location problems.

In this library, efficient algorithms are implemented to handle various types of location models. A part of the algorithms is known from the literature, whereas others are (and will be) results of current research. Most of the algorithms are based on theoretic results from graph theory, computational geometry and combinatorial optimization.

A location problem usually includes a set of existing facilities Ex_i , i = 1, ..., M, which may be situated for example in the plane or on a road network. The objective is to find one (or several) new facilities X, such that a given cost function, as for example the total travel expense, is minimized. For this purpose a weight w_i , i = 1, ..., M can be associated with each existing facility Ex_i representing for example the demand of facility Ex_i . The most common objectives are to solve either the Median problem or the Center problem, i.e. to look for a new location that minimizes either the average travel cost or the maximum travel cost.

For a detailed survey about location theory see e.g. Love et al. 1988^1 , Francis et al. 1992^2

¹R.F. Love, J.G. Morris and G.O. Wesolowsky. *Facilities Location: Models & Methods*. North Holland, New York, 1988.

²R.L. Francis, F. Leon, J. McGinnis and J.A. White. *Facility Layout and Location: An Analytical Approach, 2nd ed.* Prentice-Hall 1992.

or Hamacher 1995^3 .

In LOLA a classification scheme for location problems is used. It has been developed by Hamacher and Nickel⁴ and is described in Chapter 6. The graphical user interface (GUI) of LOLA, which is also based on this classification scheme, provides a detailed help manual to guide the user to the appropriate solution of his/her problem.

The development of LOLA is part of a larger project in location theory supported by the German Research Council (DFG) and therefore is still in process. Whereas in this version 2.0 planar location problems as described in Hamacher 1995³ and network location problems as well as some discrete problems can be solved, further network and discrete location problems will be included in an upcoming version of LOLA.

We would like to thank the DFG for the financial support that made this project possible.

How to download LOLA

You can download a copy of the source-code and some executable files from the internet:

URL http://www.mathematik.uni-kl.de/~lola

LOLA-email

For bug-reports or suggestions for improvements and further developments feel free to contact

lola@mathematik.uni-kl.de

³H.W. Hamacher. Mathematische Verfahren der Planaren Standortplanung. Vieweg 1995.

⁴H.W. Hamacher and S. Nickel: "Classification of Location Models". Technical Report in Wirtschaftsmathematik No. 19, Universität Kaiserslautern, Department of Mathematics, 1996. To appear in *Location Science*.

Part I

${\bf Getting}\,{\bf Started}\,{\bf with}\,{\bf LOLA}$

Chapter 2

A Guided Tour through the LOLA Frontend

In this chapter we give a detailed introduction to the frontend of LOLA enabling the solution of different location problems. Nevertheless, this is just a guided tour and not a complete description. For details, we refer to Chapter 7.

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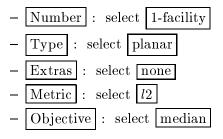
Figure 2.1: LOLA-frontend.

2.1 The classical 1-facility median problem

Assume that we want to solve the classical 1-facility-Weber problem, i.e. a planar minisumproblem with Euclidean distance. In the 5-position-classification scheme described in Chapter 6 this problem can be written as $1/P/./l_2/\Sigma$: We want to locate one new facility (1) in the plane (P) with no special assumptions (.), using the Euclidean distance as metric (l_2) and minimizing the sum of distances between the existing facilities and the new one (Σ).

In order to solve a problem of this type, follow steps a) to c).

a) Select the following options in the menue bar:



The classification string on the LOLA screen should now look like

 $1/P/\cdot/l2/\sum$.

b) Load a file with location data. The sample file "sample.loc " can be found in the directory

.../LOLA/examples

The file "sample.loc" contains the data of six existing facilities:

begin {location} [2,1] 15.00 16.00 955 [Koeln] 10.00 36.00 577 [Duesseldorf] 9.00 52.00 540 [Duisburg] 20.00 53.00 620 [Essen] 42.00 58.00 610 [Dortmund] 48.00 90.00 261 [Muenster] end {location}

The first line implies that we solve a problem in two dimensions with one objective function. The following lines contain, for every existing facility, the x-coordinate, the y-coordinate, the weight, and — optional — a symbolic name of the existing facility.

To load the file click on File in the menu bar and select Load Location. The resulting LOLA window is given in Figure 2.2.

To generate your own data files you can use either

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Figure 2.2: Loading a location file.

- any ASCII-editor to type in the data like in sample.loc according to the data file specifications, see Section 4.1.
- or the graphical editor that can be found under Graphical Edit in the File menu. In this editor the location data can be entered using the mouse.
- c) Click on computation, and LOLA will provide a window with the solution *Opt*, see Figure 2.3.

If you click on <u>View Results</u> you can see the coordinates and the objective value of the optimal solution.

2.2 A planar problem with polyhedral gauges

Now suppose that the Euclidean distance is not suitable to model the problem in our first example. Instead of the Euclidean distance function, we can use the option of LOLA to model distances by polyhedral gauges, a special case of which are block norms (polyhedral norms). In order to choose this option in the LOLA frontend, follow steps a) and b) below:

a) Choose the options in the menu analogous to the previous example, except for the metric: Under the option metric we select gauge which leads to the classification string $1/P/./gauge/\Sigma$ on the frontend.

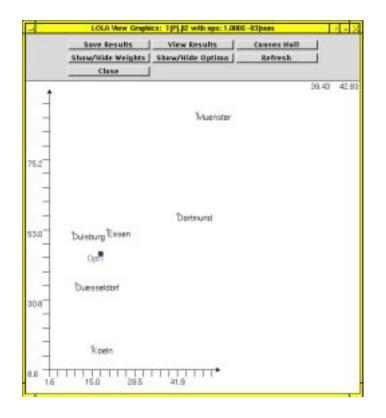


Figure 2.3: Solution-window for a problem of type $1/P/./l_2/\sum$.

b) In the next step we have to load a location file. In the case of gauge distances, the location file must provide more information since a different gauge may be used to measure the distance to each existing facility. Thus additionally to the facilities coordinates and weights, a number has to be specified corresponding to the respective gauges in a gauge-file. In Figure 2.4, an example of a gauge file "sample.gau" with two gauges is given, the first of which can be referred to as gauge(0) and the second as gauge(1). Their unit balls can be seen in Figure 2.5 and 2.6, respectively.

Remark: A (polyhedral) gauge is defined by the coordinates of its extreme points in counterclockwise order. (Note that gauges always must be convex!)

A corresponding location file "sample_gauge.loc" is given in Figure 2.7. Both files can be found in the directory

.../LOLA/examples

The solution window for this problem is depicted in Figure 2.8.

2.3 A network-problem

To solve network location problems we need the additional information of the network which is given in an adjacency matrix which is represented by an adjacency list in LOLA. This adjacency matrix defines the edge length of the network, i.e. the distances between pairs of

	Wew Gauge	
<pre>begin (polygeegelist) begin (polygeege) 1 0 0 1 -1 0 0 -1 end (polygeege) begin (polygeege) 2 0 1 1 -1 1 0 -3 end (polygeegelist) end (polygeegelist)</pre>		
	OK	

Figure 2.4: Example- gauge file with two gauges.

existing facilities, and is added to the location file. An example is given in Figure 2.9. (The corresponding location file "sample.gra" can be found in the directory .../LOLA/examples).

In this file, the existing facilities are specified and the adjacency matrix of the network G is represented in a list. Each row of this adjacency list contains the starting node, the end node and the length of the corresponding edge.

Additionally to the correct choice of the input file we have to select the option graph in the Type menu. Furthermore, in the menu Metric, we can choose between the options d(V,V) and d(V,G). Selecting d(V,V) restricts the search for an optimal solution to the nodes of the network (graph) G.

The solution window of the corresponding problem of type $1/G/./d(V, V)/\sum$ is given in Figure 2.10.

2.4 A discrete problem

For the case we want to solve a discrete problem we need more information about the type of the problem and the locations. At moment LOLA could solve the uncapacitated facility location problem (UFLP). Therefore we need information about the demand points, the supply points and the costs for moving from a supply point to demand point. In the example file "sample.dis" we see two list of facility and a cost matrix.

Before selecting the input file we have only to select option discrete in the Type menu. When pressing Computation we get a new window for choosing the type of the heuristic. We make three different heuristics and an exact algorithm for this problem available.

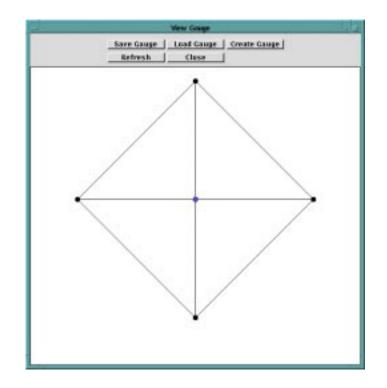


Figure 2.5: The unit ball of gauge(0) in the example file (cf. Figure 2.4).

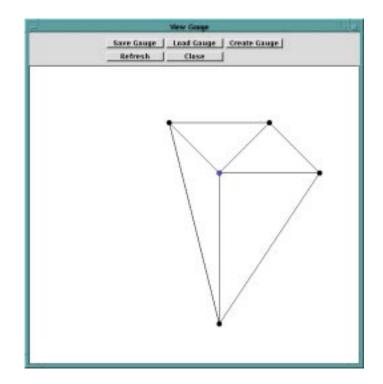


Figure 2.6: The unit ball of gauge(1) in the example file (cf. Figure 2.4).

2.4. A DISCRETE PROBLEM

View Cocation	
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OK	

Figure 2.7: A location-file containing the specification (0) and (1) for the respective gauges.

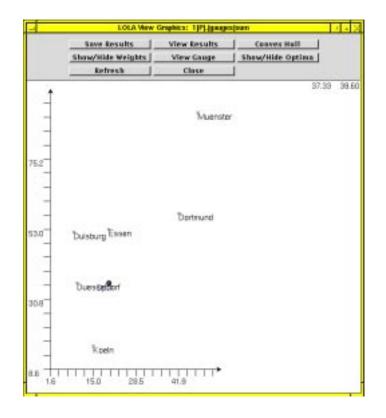


Figure 2.8: Solution window for the problem $1/P/./gauge/\sum$ defined above.



Figure 2.9: The input file for a network location problem.

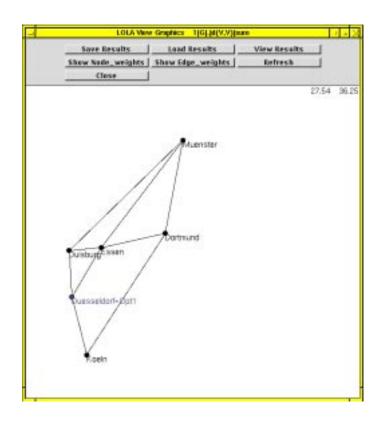


Figure 2.10: Solution window for the network problem $1/G/./d(V,V)/\sum$ defined above.

Chapter 3

Location Algorithms Available in LOLA

The algorithms available in LOLA are listed in Table 3.1.

Problem Class	Description of the Classification Scheme
$1/P/./l_1/\sum$	1-Median problem in the plane with l_1 -distances.
$\frac{1/P/./l_1/\sum}{1/P/R/l_1/\sum}$	Restricted 1-Median problem in the plane with l_1 -distances
	and forbidden region inside.
$1/P/R^c/l_1/\sum$	Restricted 1-Median problem in the plane with l_1 -distances
	and forbidden region outside.
$N/P/./l_1/\sum$	N-Median problem in the plane with l_1 -distances.
$\frac{N/P/./l_1/\sum}{1/P/./l_1/2 - \sum_{par}}$	Bi-objective 1-Median problem in the plane with l_1 -distances.
$1L/P/./l_1/\sum$	Locating 1 line in the plane wrt. l_1 -distances and the median
	objective function.
$1L/P/R = convpolyhed/l_1/\sum$	Locating 1 line in the plane wrt. l_1 -distances and the
	median objective function with convex polyhedral forbidden regions.
$\frac{1/P/./l_2/\sum}{1/P/R = convpolyhed/l_2/\sum}$	1-Median problem in the plane with Euclidean distances.
$1/P/R = convpolyhed/l_2/\sum$	Restricted 1-Median problem in the plane with
	l_2 -distances and forbidden region inside.
$1/P/B/l_2/\sum$	Restricted 1-Median problem in the plane with
	l_2 -distances and barriers.
$\frac{N/P/./l_2/\sum}{1L/P/./l_2/\sum}$	N-Median problem in the plane with Euclidean distances.
$1L/P/./l_2/\sum$	Locating 1 line in the plane wrt. Euclidean distances
	and the median objective function.
$1L/P/w_i = 1/l_2/\sum$	Locating 1 line in the plane wrt. Euclidean distances and the
	median objective function where all weights are equal to 1.
$1L/P/R = convpolyhed/l_2/\sum$	Locating 1 line in the plane wrt. Euclidean distances
	and the median objective function with convex
	polyhedral forbidden regions.
$1/P/./l_2^2/\sum$	1-Median problem in the plane with
	squared Euclidean distances.

$\begin{split} 1/P/R/l_2/\Sigma & \text{Restricted 1-Median problem in the plane with squared Euclidean distances and forbidden region inside. \\ 1/P/R^2/l_2^2/\Sigma & \text{Restricted 1-Median problem in the plane with squared Euclidean distances and forbidden region outside. \\ N/P!./l_2^2/\Sigma & N-Median problem in the plane with squared Euclidean distances. \\ 1/P!./l_2^2/Q - \Sigma_{par} & Q-objective 1-Median problem in the plane with squared Euclidean distances. \\ 1/P!./l_p/\Sigma & 1-Median problem in the plane with l_p-distances (1$		
$\begin{aligned} & \text{and forbidden region inside.} \\ & \text{Restricted 1-Median problem in the plane} \\ & \text{with squared Euclidean distances} \\ & \text{and forbidden region outside.} \\ & N/P/./l_2^2/\Sigma & N-Median problem in the plane \\ & \text{with squared Euclidean distances.} \\ & 1/P/.l_2^n/Q - \Sigma_{par} & Q-objective 1-Median problem in the plane \\ & \text{with squared Euclidean distances.} \\ & 1/P/.l_p^n/\Sigma & 1-Median problem in the plane with l_p-distances (1$	$1/P/R/l_2^2/\sum$	Restricted 1-Median problem in the plane
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$ \begin{array}{c c} N/P/./l_{\infty}/\sum & N\mbox{-Median problem in the plane with } l_{\infty}\mbox{-distances.} \\ \hline 1/P/./l_{\infty}/2 - \sum_{par} & \mbox{Bi-objective 1-Median problem in the plane with } l_{\infty}\mbox{-distances.} \\ \hline 1L/P/./l_{\infty}/\sum & \mbox{Locating 1 line in the plane wrt. } l_{\infty}\mbox{-distances} \\ \hline and the median objective function. \\ \hline 1L/P/R = convpolyhed/l_{\infty}/\sum & \mbox{Locating 1 line in the plane wrt. } l_{\infty}\mbox{-distances} \\ \hline and the median objective function with \\ \hline convex polyhedral forbidden regions. \\ \hline 1/P/./\gamma/2 - \sum_{par} & \mbox{Bi-objective 1-Median problem in the plane with polyhedral gauges.} \\ \hline 1L/P/./\gamma_{B}/\sum & \mbox{Locating 1 line in the plane wrt. block norms \\ \hline and the median objective function. \\ \hline 1L/P/./\gamma_{B}/\sum & \mbox{Locating 1 line in the plane wrt. block norms \\ \hline and the median objective function. \\ \hline 1L/P/R = convpolyhed/\gamma_{B}/\sum & \mbox{Locating 1 line in the plane wrt. block norms \\ \hline and the median objective function. \\ \hline 1/P//l_1/max & \mbox{L-center problem in the plane with } l_1\mbox{-distances.} \\ \hline 1/P/R = convex/l_1/max & \mbox{L-center problem in the plane with } l_1\mbox{-distances.} \\ \hline 1/P/R = convex/l_1/max & \mbox{L-center problem in the plane with } l_1\mbox{-distances.} \\ \hline 1/P/R = convex/l_1/max & \mbox{L-center problem in the plane with } l_1\mbox{-distances.} \\ \hline 1/P/R = convex/l_1/max & \mbox{L-center problem in the plane with } l_1\mbox{-distances.} \\ \hline 1/P/R = convex/l_1/max & \mbox{L-center problem in the plane with } l_1\mbox{-distances with } \\ \hline 1/P/R = convex/l_1/max & \mbox{L-center problem in the plane with } l_1\mbox{-distances with } \\ \hline 1\mbox{-distances with } \\ \hline 1-distan$	$1/T/R/l_{\infty}/\Sigma$	
$\begin{array}{c c} 1/P/./l_{\infty}/2-\sum_{par} & \mbox{Bi-objective 1-Median problem in the plane with } l_{\infty}\mbox{-distances.} \\ 1L/P/./l_{\infty}/\sum & \mbox{Locating 1 line in the plane wrt. } l_{\infty}\mbox{-distances} \\ & \mbox{and the median objective function.} \\ 1L/P/R = convpolyhed/l_{\infty}/\sum & \mbox{Locating 1 line in the plane wrt. } l_{\infty}\mbox{-distances} \\ & \mbox{and the median objective function with} \\ & \mbox{convex polyhedral forbidden regions.} \\ \hline 1/P/./\gamma/2 - \sum_{par} & \mbox{Bi-objective 1-Median problem in the plane with polyhedral gauges.} \\ \hline 1/P/./\gamma_B/\sum & \mbox{Locating 1 line in the plane wrt. block norms \\ & \mbox{and the median objective function.} \\ \hline 1L/P/R = convpolyhed/\gamma_B/\sum & \mbox{Locating 1 line in the plane wrt. block norms \\ & \mbox{and the median objective function.} \\ \hline 1/P/.l_1/max & \mbox{1-center problem in the plane with } l_1\mbox{-distances.} \\ \hline 1/P/R = convex/l_1/max & \mbox{1-center problem in the plane with } l_1\mbox{-distances.} \\ \hline 1/P/R = convex/l_1/max & \mbox{1-center problem in the plane with } l_1\mbox{-distances.} \\ \hline 1/P/R = convex/l_1/max & \mbox{1-center problem in the plane with } l_1\mbox{-distances.} \\ \hline 1/P/R = convex/l_1/max & \mbox{1-center problem in the plane with } l_1\mbox{-distances.} \\ \hline 1/P/R = convex/l_1/max & \mbox{1-center problem in the plane with } l_1\mbox{-distances.} \\ \hline 1/P/R = convex/l_1/max & \mbox{1-center problem in the plane with } l_1\mbox{-distances.} \\ \hline 1/P/R = convex/l_1/max & \mbox{1-center problem in the plane with } l_1\mbox{-distances.} \\ \hline 1/P/R = convex/l_1/max & \mbox{1-center problem in the plane with } l_1\mbox{-distances.} \\ \hline 1/P/R = convex/l_1/max & \mbox{1-center problem in the plane with } l_1\mbox{-distances.} \\ \hline 1/P/R = convex/l_1/max & \mbox{1-center problem in the plane with } l_1\mbox{-distances with } \\ \hline 1/P/R = convex/l_1/max & \mbox{1-center problem in the plane with } l_1\mbox{-distances with } \\ \hline 1/P/R = convex/l_1/max & \mbox{1-center problem in the plane with } l_1\mbox{-distances with } \\ \hline 1/P/R = convex/l_1/max & \mbo$	$N/D//l / \Sigma$	
$\begin{array}{ c c c c } & \text{and the median objective function.} \\ \hline 1L/P/R = convpolyhed/l_{\infty}/\sum & \text{Locating 1 line in the plane wrt. } l_{\infty}\text{-distances} \\ & \text{and the median objective function with} \\ & \text{convex polyhedral forbidden regions.} \\ \hline 1/P/./\gamma/\sum & 1\text{-Median problem in the plane with polyhedral gauges.} \\ \hline 1/P/./\gamma/2 - \sum_{par} & \text{Bi-objective 1-Median problem in the plane} \\ & \text{with polyhedral gauges.} \\ \hline 1L/P/./\gamma_B/\sum & \text{Locating 1 line in the plane wrt. block norms} \\ & \text{and the median objective function.} \\ \hline 1L/P/R = convpolyhed/\gamma_B/\sum & \text{Locating 1 line in the plane wrt. block norms} \\ & \text{and the median objective function.} \\ \hline 1/P/.l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances.} \\ \hline 1/P/w_i = 1/l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances where} \\ & \text{all weights are equal to 1.} \\ \hline 1/P/R = convex/l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances with} \\ & \text{convex polyhedral forbidden regions.} \\ \hline 1/P/R = convex/l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances with} \\ & \text{convex polyhedral forbidden regions.} \\ \hline 1/P/R = convex/l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances with} \\ & \text{convex polyhedral forbidden regions.} \\ \hline 1/P/R = convex/l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances with} \\ & \text{convex polyhedral forbidden regions.} \\ \hline 1/P/R = convex/l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances with} \\ & \text{convex polyhedral forbidden regions.} \\ \hline 1/P/R = convex/l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances with} \\ & \text{convex polyhedral forbidden regions.} \\ \hline 1/P/R = convex/l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances with} \\ & \text{convex polyhedral forbidden regions.} \\ \hline 1/P/R = convex/l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances with} \\ & \text{convex polyhedral forbidden regions.} \\ \hline 1/P/R = convex/l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances with} \\ & convex polyhedral forbidden regi$	$\frac{N/P/./l_{\infty}/\Sigma}{1/D/./l_{\omega}/\Sigma}$	
$\begin{array}{ c c c c } & \text{and the median objective function.} \\ \hline 1L/P/R = convpolyhed/l_{\infty}/\sum & \text{Locating 1 line in the plane wrt. } l_{\infty}\text{-distances} \\ & \text{and the median objective function with} \\ & \text{convex polyhedral forbidden regions.} \\ \hline 1/P/./\gamma/\sum & 1\text{-Median problem in the plane with polyhedral gauges.} \\ \hline 1/P/./\gamma/2 - \sum_{par} & \text{Bi-objective 1-Median problem in the plane} \\ & \text{with polyhedral gauges.} \\ \hline 1L/P/./\gamma_B/\sum & \text{Locating 1 line in the plane wrt. block norms} \\ & \text{and the median objective function.} \\ \hline 1L/P/R = convpolyhed/\gamma_B/\sum & \text{Locating 1 line in the plane wrt. block norms} \\ & \text{and the median objective function.} \\ \hline 1/P/.l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances.} \\ \hline 1/P/w_i = 1/l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances where} \\ & \text{all weights are equal to 1.} \\ \hline 1/P/R = convex/l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances with} \\ & \text{convex polyhedral forbidden regions.} \\ \hline 1/P/R = convex/l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances with} \\ & \text{convex polyhedral forbidden regions.} \\ \hline 1/P/R = convex/l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances with} \\ & \text{convex polyhedral forbidden regions.} \\ \hline 1/P/R = convex/l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances with} \\ & \text{convex polyhedral forbidden regions.} \\ \hline 1/P/R = convex/l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances with} \\ & \text{convex polyhedral forbidden regions.} \\ \hline 1/P/R = convex/l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances with} \\ & \text{convex polyhedral forbidden regions.} \\ \hline 1/P/R = convex/l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances with} \\ & \text{convex polyhedral forbidden regions.} \\ \hline 1/P/R = convex/l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances with} \\ & \text{convex polyhedral forbidden regions.} \\ \hline 1/P/R = convex/l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances with} \\ & convex polyhedral forbidden regi$	$\frac{1/P/./l_{\infty}/2 - \sum_{par}}{1/P/./l_{\infty}/2}$	
$\begin{array}{c c} 1L/P/R = convpolyhed/l_{\infty}/\sum & \text{Locating 1 line in the plane wrt. } l_{\infty}\text{-distances} \\ & \text{and the median objective function with} \\ & \text{convex polyhedral forbidden regions.} \\ \hline 1/P/./\gamma/\sum & 1\text{-Median problem in the plane with polyhedral gauges.} \\ & 1/P/./\gamma/2 - \sum_{par} & \text{Bi-objective 1-Median problem in the plane} \\ & \text{with polyhedral gauges.} \\ \hline 1L/P/./\gamma_B/\sum & \text{Locating 1 line in the plane wrt. block norms} \\ & \text{and the median objective function.} \\ \hline 1L/P/R = convpolyhed/\gamma_B/\sum & \text{Locating 1 line in the plane wrt. block norms} \\ & \text{and the median objective function.} \\ \hline 1/P/./l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances.} \\ \hline 1/P/w_i = 1/l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances where} \\ & \text{all weights are equal to 1.} \\ \hline 1/P/R = convex/l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances with} \\ & \text{convex polyhedral forbidden regions.} \\ \hline \end{array}$	$1L/P/./l_{\infty}/\sum$	
and the median objective function with convex polyhedral forbidden regions. $1/P/./\gamma/\Sigma$ 1-Median problem in the plane with polyhedral gauges. $1/P/./\gamma/2 - \sum_{par}$ Bi-objective 1-Median problem in the plane with polyhedral gauges. $1L/P/./\gamma_B/\Sigma$ Locating 1 line in the plane wrt. block norms and the median objective function. $1L/P/R = convpolyhed/\gamma_B/\Sigma$ Locating 1 line in the plane wrt. block norms and the median objective function. $1/P/./l_1/max$ 1-center problem in the plane with l_1 -distances. $1/P/w_i = 1/l_1/max$ 1-center problem in the plane with l_1 -distances where all weights are equal to 1. $1/P/R = convex/l_1/max$ 1-center problem in the plane with l_1 -distances with convex polyhedral forbidden regions.		
$\begin{tabular}{ c c c c c } \hline convex polyhedral forbidden regions. \\ \hline $1/P/./\gamma/2 - \sum_{par}$ I-Median problem in the plane with polyhedral gauges. \\ \hline $1/P/./\gamma/2 - \sum_{par}$ Bi-objective 1-Median problem in the plane with polyhedral gauges. \\ \hline $1L/P/./\gamma_B/\Sigma$ Locating 1 line in the plane wrt. block norms and the median objective function. \\ \hline $1L/P/R = convpolyhed/\gamma_B/\Sigma$ Locating 1 line in the plane wrt. block norms and the median objective function with convex polyhedral forbidden regions. \\ \hline $1/P/.l_1/max$ I-center problem in the plane with l_1-distances. \\ \hline $1/P/w_i = 1/l_1/max$ I-center problem in the plane with l_1-distances where all weights are equal to 1. \\ \hline $1/P/R = convex/l_1/max$ I-center problem in the plane with l_1-distances with convex polyhedral forbidden regions. \\ \hline $1/P/R = convex/l_1/max$ I-center problem in the plane with l_1-distances with convex polyhedral forbidden regions. \\ \hline $1/P/R = convex/l_1/max$ I-center problem in the plane with l_1-distances with convex polyhedral forbidden regions. \\ \hline $1/P/R = convex/l_1/max$ I-center problem in the plane with l_1-distances with convex polyhedral forbidden regions. \\ \hline $1/P/R = convex/l_1/max$ I-center problem in the plane with l_1-distances with convex polyhedral forbidden regions. \\ \hline $1/P/R = convex/l_1/max$ I-center problem in the plane with l_1-distances with convex polyhedral forbidden regions. \\ \hline $1/P/R = convex/l_1/max$ I-center problem in the plane with l_1-distances with convex polyhedral forbidden regions. \\ \hline $1/P/R = convex/l_1/max$ I-center problem in the plane with l_1-distances with convex polyhedral forbidden regions. \\ \hline $1/P/R = convex/l_1/max$ I-center problem in the plane with l_1-distances with convex polyhedral forbidden regions. \\ \hline $1/P/R = convex/l_1/max$ I-center problem in the plane with l_1-distances with convex polyhedral forbidden regions. \\ \hline $1/P/R = convex/l_1/max$ I-center problem in the plane with l_1-distances with convex polyhedral forbidden regions. \\ \hline $1/P/R = convex/l_1/$	$1L/P/R = convpolyhed/l_{\infty}/\sum$	
$1/P/./\gamma/\Sigma$ 1-Median problem in the plane with polyhedral gauges. $1/P/./\gamma/2 - \sum_{par}$ Bi-objective 1-Median problem in the plane with polyhedral gauges. $1L/P/./\gamma_B/\Sigma$ Locating 1 line in the plane wrt. block norms and the median objective function. $1L/P/R = convpolyhed/\gamma_B/\Sigma$ Locating 1 line in the plane wrt. block norms and the median objective function with convex polyhedral forbidden regions. $1/P/./l_1/max$ 1-center problem in the plane with l_1 -distances. $1/P/w_i = 1/l_1/max$ 1-center problem in the plane with l_1 -distances where all weights are equal to 1. $1/P/R = convex/l_1/max$ 1-center problem in the plane with l_1 -distances with convex polyhedral forbidden regions.		
with polyhedral gauges. $1L/P/./\gamma_B/\Sigma$ Locating 1 line in the plane wrt. block norms and the median objective function. $1L/P/R = convpolyhed/\gamma_B/\Sigma$ Locating 1 line in the plane wrt. block norms and the median objective function with convex polyhedral forbidden regions. $1/P/./l_1/max$ 1-center problem in the plane with l_1 -distances. $1/P/w_i = 1/l_1/max$ 1-center problem in the plane with l_1 -distances where all weights are equal to 1. $1/P/R = convex/l_1/max$ 1-center problem in the plane with l_1 -distances with convex polyhedral forbidden regions.		convex polyhedral forbidden regions.
with polyhedral gauges. $1L/P/./\gamma_B/\Sigma$ Locating 1 line in the plane wrt. block norms and the median objective function. $1L/P/R = convpolyhed/\gamma_B/\Sigma$ Locating 1 line in the plane wrt. block norms and the median objective function with convex polyhedral forbidden regions. $1/P/./l_1/max$ 1-center problem in the plane with l_1 -distances. $1/P/w_i = 1/l_1/max$ 1-center problem in the plane with l_1 -distances where all weights are equal to 1. $1/P/R = convex/l_1/max$ 1-center problem in the plane with l_1 -distances with convex polyhedral forbidden regions.	$1/P/./\gamma/\sum$	1-Median problem in the plane with polyhedral gauges.
with polyhedral gauges. $1L/P/./\gamma_B/\Sigma$ Locating 1 line in the plane wrt. block norms and the median objective function. $1L/P/R = convpolyhed/\gamma_B/\Sigma$ Locating 1 line in the plane wrt. block norms and the median objective function with convex polyhedral forbidden regions. $1/P/./l_1/max$ 1-center problem in the plane with l_1 -distances. $1/P/w_i = 1/l_1/max$ 1-center problem in the plane with l_1 -distances where all weights are equal to 1. $1/P/R = convex/l_1/max$ 1-center problem in the plane with l_1 -distances with convex polyhedral forbidden regions.	$1/P/./\gamma/2 - \sum_{max}$	Bi-objective 1-Median problem in the plane
$1L/P/./\gamma_B/\Sigma$ Locating 1 line in the plane wrt. block norms and the median objective function. $1L/P/R = convpolyhed/\gamma_B/\Sigma$ Locating 1 line in the plane wrt. block norms and the median objective function with convex polyhedral forbidden regions. $1/P/./l_1/max$ 1-center problem in the plane with l_1 -distances. $1/P/w_i = 1/l_1/max$ 1-center problem in the plane with l_1 -distances where all weights are equal to 1. $1/P/R = convex/l_1/max$ 1-center problem in the plane with l_1 -distances with convex polyhedral forbidden regions.		with polyhedral gauges.
$\begin{array}{ c c c c c } & \text{and the median objective function.} \\ \hline 1L/P/R = convpolyhed/\gamma_B/\sum & \text{Locating 1 line in the plane wrt. block norms} \\ & \text{and the median objective function with} \\ & \text{convex polyhedral forbidden regions.} \\ \hline 1/P/./l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances.} \\ \hline 1/P/w_i = 1/l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances where} \\ & \text{all weights are equal to 1.} \\ \hline 1/P/R = convex/l_1/max & 1\text{-center problem in the plane with } l_1\text{-distances with} \\ & \text{convex polyhedral forbidden regions.} \\ \hline \end{array}$	$1L/P/./\gamma_B/\Sigma$	
$\begin{array}{ c c c c c c } 1L/P/R = convpolyhed/\gamma_B/\sum & \mbox{Locating 1 line in the plane wrt. block norms} \\ & \mbox{and the median objective function with} \\ & \mbox{convex polyhedral forbidden regions.} \\ \hline 1/P/./l_1/max & \mbox{1-center problem in the plane with } l_1\mbox{-distances.} \\ & \mbox{1/P/w}_i = 1/l_1/max & \mbox{1-center problem in the plane with } l_1\mbox{-distances where} \\ & \mbox{all weights are equal to 1.} \\ & \mbox{1/P/R} = convex/l_1/max & \mbox{1-center problem in the plane with } l_1\mbox{-distances with} \\ & \mbox{convex polyhedral forbidden regions.} \\ \hline \end{array}$		
and the median objective function with convex polyhedral forbidden regions. $1/P/./l_1/max$ 1-center problem in the plane with l_1 -distances. $1/P/w_i = 1/l_1/max$ 1-center problem in the plane with l_1 -distances where all weights are equal to 1. $1/P/R = convex/l_1/max$ 1-center problem in the plane with l_1 -distances with convex polyhedral forbidden regions.	$1L/P/R = convpoluted/\gamma_P/\Sigma$	
convex polyhedral forbidden regions. $1/P/./l_1/max$ 1-center problem in the plane with l_1 -distances. $1/P/w_i = 1/l_1/max$ 1-center problem in the plane with l_1 -distances where all weights are equal to 1. $1/P/R = convex/l_1/max$ 1-center problem in the plane with l_1 -distances with convex polyhedral forbidden regions.		
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all weights are equal to 1. $1/P/R = convex/l_1/max$ 1-center problem in the plane with l_1 -distances with convex polyhedral forbidden regions.	$1/\Gamma/./l_1/max$	
$\frac{1/P/R = convex/l_1/max}{convex \text{ polyhedral forbidden regions.}}$ 1-center problem in the plane with l_1 -distances with	$1/P/w_i = 1/l_1/max$	
convex polyhedral forbidden regions.	1/D/D	
	$1/P/R = convex/l_1/max$	
$N/P/./l_1/max$ N-center problem in the plane with l_1 -distances. $1L/P/./l_1/max$ Locating 1 line in the plane wrt. l_1 -distances and the		
$1L/P/./l_1/max$ Locating 1 line in the plane wrt. l_1 -distances and the	$N/P/./l_1/max$	
	$1L/P/./l_1/max$	Locating 1 line in the plane wrt. l_1 -distances and the

	center objective function.
$1/P/./l_2/max$	1-center problem in the plane with Euclidean distances.
$\frac{1/P/R/l_2/max}{1/P/R/l_2/max}$	Restricted 1-center problem in the plane with
, , , , 2,	Euclidean distances.
$1L/P/./l_2/max$	Locating 1 line in the plane wrt. Euclidean distances
, , , , , , , ,	and the center objective function.
$1L/P/./l_p/max$	Locating 1 line in the plane wrt. l_p -distances $(1$
	and the center objective function. $(1 + p)$
$1/P/./l_{\infty}/max$	1-center problem in the plane with l_{∞} -distances.
$\frac{1/P/./l_{\infty}/max}{1/P/w_i = 1/l_{\infty}/max}$	1-center problem in the plane with l_{∞} -distances
	where all weights are equal to 1.
$1/P/R = convex/l_{\infty}/max$	1-center problem in the plane with l_{∞} -distances with
	convex polyhedral forbidden regions.
$\frac{N/P/./l_{\infty}/max}{1L/P/./l_{\infty}/max}$	N-center problem in the plane with l_{∞} -distances.
$1L/P/./l_{\infty}/max$	Locating 1 line in the plane wrt. l_{∞} -distances and the
	center objective function.
$1/P/./\gamma/\max$	1-Center problem in the plane with polyhedral gauges.
$1/P/R/\gamma/\max$	1-Center problem in the plane with polyhedral gauges and forbidden regio
$1L/P/./\gamma_B/\max$	Locating 1 line in the plane wrt. block norms and the
	center objective function.
$1/G_D/./d(V,V)/\sum$	1-Median problem on a directed graph,
	restricted to the nodes of G_D .
$\frac{1/G/./d(V,V)/\sum}{1/G/./d(V,G)/\sum}$	1-Median problem on a graph, restricted to the nodes of G .
$1/G/./d(V,G)/\sum$	1-Median problem on a graph where the optimal
	solution may be anywhere on G .
$\frac{1/T/./d(V,V)/\sum}{1/T/./d(V,T)/\sum}$	1-Median problem on a tree T , restricted to the nodes of T .
$1/1'/./a(V, 1)/\sum$	1-Median problem on a tree T where the optimal
$\frac{1/C}{d(VC)/2}$	solution may be anywhere on T . Bi-objective 1-Median problem on a graph G .
$\frac{1/G/./d(V,G)/2 - \sum_{par}}{1/G/./d(V,G)/Q}$	Q-objective 1-Median problem on a graph G .
$\frac{1/G/./d(V,G)/Q - \sum_{par}}{1/C/./d(V,V)/Q - \sum_{par}}$	Q-objective 1-Median problem on a graph G . Q-objective 1-Median problem on a graph G ,
$\frac{1/G/./d(V,V)/Q - \sum_{par}}{}$	Q-objective 1-Median problem on a graph G , restricted to the nodes of G .
$\frac{1/G_{\rm D}}{d(V G)} = \Sigma$	Q -objective 1-Median problem on a directed graph G_D .
$\frac{1/G_D/./d(V,G)/Q - \sum_{par}}{1/G_D/./d(V,V)/Q - \sum_{par}}$	Q -objective 1-Median problem on a directed graph G_D . Q -objective 1-Median problem on a directed graph G_D ,
$1/GD/./G(v, v)/G$ $\angle par$	restricted to the nodes of G_D .
$1/G/./d(V,G)/Q - \sum_{lex}$	Q-objective 1-Median problem on a graph G wrt. the
$1/(1/(1/(1/(1/(2))))) \leq 2 lex$	lexicographic ordering where the optimal solution may be
	anywhere on the graph G .
$1/G/./d(V,V)/Q - \sum_{lex}$	Q-objective 1-Median problem on a graph G ,
	restricted to the nodes of G wrt. the lexicographic ordering.
$1/G_D/./d(V,V)/Q - \sum_{lex}$	Q-objective 1-Median problem on a directed graph G wrt. the
	lexicographic ordering where the optimal solution may be
	anywhere on the graph.
$1/G_D/./d(V,V)/Q - \sum_{lex}$	Q-objective 1-Median problem on a directed graph G ,
	restricted to the nodes of G wrt. the lexicographic ordering.

$1/G_D/./d(V,G)/\max$	1-Center problem on a directed graph G_D .
$1/G_D/./d(V,V)/\max$	1-Center problem on a directed graph,
	restricted to the nodes of G_D .
$1/G/./d(V,V)/\max$	1-Center problem on a graph G , restricted to the nodes of G .
$1/G/./d(V,G)/\max$	1-Center problem on a graph G where the optimal
	solution may be anywhere on G .
$1/T/./d(V,V)/\max$	1-Center problem on a tree T , restricted to the nodes of T .
$1/T/./d(V,T)/\max$	1-Center problem on a tree T where the optimal
	solution may be anywhere on T .
$1/G_D/./d(V,V)/Q - \max_{par}$	Q-objective 1-Center problem on a directed graph G_D ,
	restricted to the nodes of G_D .
$1/G_D/./d(V,G)/Q - \max_{par}$	Q -objective 1-Center problem on a directed graph G_D where
	the optimal solution may be anywhere on the directed graph G_D .
$1/G/./d(V,V)/Q - \max_{lex}$	Q-objective 1-Center problem on a graph G ,
	restricted to the nodes of G , wrt. the lexicographic ordering.
$1/G_D/./d(V,V)/Q - \max_{lex}$	Q-objective 1-Center problem on a directed graph G ,
	restricted to the nodes of G , wrt. the lexicographic ordering.
$N/G/./d(V,V)/\sum$	N-Median problem on a graph G , restricted to the nodes of G .
$N/G/./d(V,V)/\max$	N-Center problem on a graph G , restricted to the nodes of G .
#/D/././.	Uncapacitated facility location problem.
	Table 3.1. Algorithms of LOLA

Table 3.1: Algorithms of LOLA

Chapter 4

Format of the Input Data

The system LOLA reads and interprets problem data for location problems in a descriptive language especially designed for that task. Furtheron a graphical editor is available to convert graphical input into that language.

Note that the blanks in the environment specifications as given below can not be ommitted!

4.1 File Type *loc* (containing location data)

 x_{ij} j-th coordinate of the *i*-th facility

- w_{ij} For <u>N-Facilities</u>-problems: For each new facility there must be a weight representing the importance (demand) of this new facility wrt. the existing facilities. The value w_{ij} represents the weight of the *j*-th new facility wrt. the *i*-th existing facility. Note that in the case that N = 1, i.e. for 1-facility problems, only one weight w_i has to be specified for each existing facility.
 - For Q-median or Q-center problems: w_{ij} represents the weight (demand, importance) of the existing facility *i* with respect to the *j*-th criterion (objective).
- d: Dimension of the facilities.
- **Q:** For N-Facilities Problems: Q is the dimension of the weights, which is in this case equal to the number N of new locations.

For Q-median or Q-center problems: The number of criteria (objectives) according to which the problem is to be solved.

As an example consider a planar 1-facility problem with Median-Objective. Then [d, Q] is assigned the values [2,1], i.e. we consider a problem in two dimensions and we need one weight per existing facility in order to find the new location. When the graphical editor is used, the weight is set to 1 by default.

4.2 File Type mat (containing the information about interactions between the new facilities in case of N-Facilities problems)

```
begin {matrix} [N]

w_{11} \cdots w_{1N}

\vdots

w_{N1} \cdots w_{NN}

end {matrix}
```

The entries w_{ij} represent the interaction (weight) between the new locations. The value N specifies the number of new facilities sought. Note that a matrix file of this type is only needed for N-Facilities problems where $N \ge 2$.

4.3 File Type *res* (containing the information about restrictions)

In case of two dimensional, planar location problems, restrictions (forbidden regions or barriers for the new locations) can be introduced to the problem using files of type *res*:

```
begin {restriction} [2]
begin {polyhedron} [m]
        (x_i, y_i) represent the (two-dimensional) coordinates
x_1 \ y_1
        of the i-th extreme point of a polyhedron.
x_2 \, y_2
  ÷
        Note that this polyhedron may also be non-convex.
x_n y_n
end {polyhedron}
begin {conpolyhedron} [m]
x_1 \, y_1
        This environment should be alternatively used in case
        of convex polyhedral restrictions.
x_2 \ y_2
  ÷
x_n y_n
end {conpolyhedron}
```

```
begin {circle} [m]
x \ y \ r The point (x, y) specifies the center-point of the circle and r its radius.
end {circle}
begin {rectangle} [0]
                    In the case that a restriction is represented by a rectangle,
                    (x_1, y_1) specifies the lower left corner of the rectangle.
x_1 y_1 \Delta x \Delta y \alpha \quad \Delta x \text{ and } \Delta y \text{ specify the height and width,}
                    respectively, and \alpha is the angle between the
                    rectangles lower side and the x-axis.
end {rectangle}
begin {segment} [inf]
         A segment is represented by its two end points
x_1 \, y_1
        (x_1, y_1) and (x_2, y_2).
x_2 y_2
  :
x_n y_n
end {segment}
```

```
end {restriction}
```

Remark The coefficient m indicates the type of restriction:

```
0: restriction is a forbidden region.
```

```
inf: restriction is a barrier.
```

Example In the following example the input data for a 1-facility problem in the plane (\mathbb{R}^2) is given where additionally a circular restriction is taken into account. The location file of type *loc* is given by

```
begin {location} [2,1]
2 2 1 [OrtA]
5 3 1 [OrtB]
8 3 1 [OrtC]
4 4 1 [OrtD]
end {location}
```

If we select the option restrictions in the Specials menu and then the restriction type circle, a possible choice of a restriction-file is

begin {restriction} [2]
begin {circle} [0]

4 4 2 end {circle} end {restriction}

In Figure 4.1 the solution window of a 1-median problem in the plane with the l_{∞} metric is given using this input data.

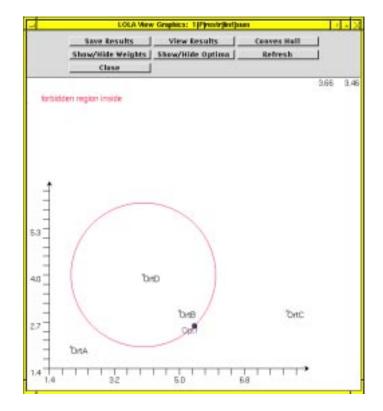


Figure 4.1: Solution window of a problem of type $1/P/R = C/l_{\infty}/\sum$ with a circular restriction.

Figure 4.2 shows the solution window of the same problem with a different (polyhedral) restriction.

Note that in the current version of LOLA only the above specified types of restrictions (i.e. polyhedral or circular sets) can be implemented. Nevertheless it is possible to include several restrictions of the same type into one restriction file whereas other types may be ommitted. The individual restriction regions have to be pairwise disjoint!

4.4 File Type gauge (containing the data of polyhedral gauges)

The input format for files of the type *polygauge* consists of a list of points which define a convex polyhedron containing the origin in its interior. The points in this list must be sorted in counterclockwise order. Several polyhedral gauges may be collected in a file of type *polygaugelist*.

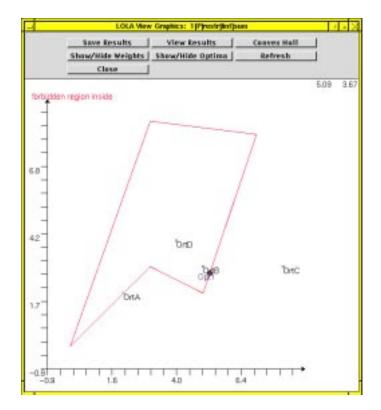


Figure 4.2: Solution window of a problem of type $1/P/R = P/l_{\infty}/\sum$ with a (non-convex) polyhedral restriction.

```
begin {polygaugelist}
begin { polygauge}
x_1 y_1
\vdots
x_n y_n
end {polygauge}
\vdots
begin {polygauge}
x_1 y_1
\vdots
x_1 y_1
\vdots
x_m y_m
end {polygauge}
end {polygaugelist}
```

4.5 File Type graph (containing the location and network information for network problems)

The input format for network location problems consists of a *location*-file and a file representing the adjacency matrix of the network (graph) in an *adjacencylist*. For this

purpose the format *adjlist* is provided where the edges of the corresponding network can be specified using their starting node (source node) and their end node (target node). The information of the existing facilities and the other nodes of the network is stored using the *location* format. Here the nodes can be specified by their (*d*-dimensional) coordinates which allows the use of location data from problems of planar type (cf. Section 4.1). They can be alternatively assigned the attribute NC, i.e. "no coordinates" have to be specified. Nodes of the network not representing an existing facility can be included in this list by setting their weights w_{ij} equal to zero.

1. Coordinate format of the location file:

2. No-coordinate format of the location file:

The adjacency list, which is additionally needed for network location problems, contains the definition and the lengths of the edges. Two different options are available: The edges can be defined by the numbers of the source- and target node, or by the symbolic names of the respective nodes.

3. Number-format of the adjacency list

```
\begin{array}{ccc} \texttt{begin} \{\texttt{adjlist}\} \\ source_1 target_1 & ew_1 \\ & \vdots & \vdots \\ source_n target_n & ew_n \\ \texttt{end} \{\texttt{adjlist}\} \end{array}
```

 ew_i : Length of the *i*-th edge running from

 $source_i$: number of the starting node of the *i*-th edge in the location file to $target_i$: number of the end node of the *i*-th edge in the location file.

4. Symbolic name-format of the adjacency list

 ew_i : Length of the *i*-th edge running from

 $sourcename_i$: symbolic name of the starting node of the *i*-th edge in the location file to

 $target_i$: symbolic name of the end node of the *i*-th edge in the location file

Example If we choose the option graph in the Type menu and the option d(V,V) in the Metric menu, a data file for the corresponding network location problem of type $1/G/./d(V,V)/\Sigma$ is given in Figure 4.3. An alternative representation of the same data is shown in Figures 4.5 and 4.6. The solution of this problem is given in Figure 4.4.



Figure 4.3: Input file for a network location problem - containing the location file in the coordinate-format and the adjacency matrix in the name-format.

The same solution we would get with the Input File shown in Figure 4.5.

4.6 File Type *dis* (containing data for discrete location problems)

An input format for a discrete location problem consists of three units: demand points, supply points and costs for moving from a supply point to a demand point. Each of the m demand points is specified by two coordinates and a weight for demand b. Optionally, a symbolic name may be given to a demand point.

Each of the n supply points is specified by two coordinates. However, the number of weights must be 1 or 2. This is given by a number p in the **begin** line. If there is only one weight

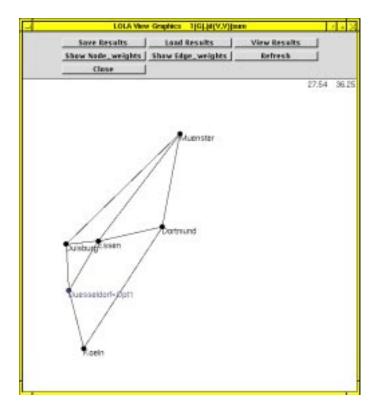


Figure 4.4: Solution window for the network location problem of type $1/G/./d(V,V)/\sum$ with the input data given in Figure 4.3.

then this is associated with the fixed costs for building a real supply depot in this location. The second weight represents the capacity constraints for the supply point.

If no list of supply points is given, then the demand points are at the same time supply points. Moreover, b_i denotes the fixed costs for location *i*.

The third input data is the $m \times n$ matrix for the costs.

```
begin {costmatrix}

c_{11} \cdots c_{1n}

\vdots \vdots \vdots \vdots

c_{m1} \cdots c_{mn}

end {costmatrix}

end {discrete}
```

View Graph	
<pre>hegin (lolegraph) hegin (lolegraph) hegin (location) [2.1] 13 00 16 00 455 [Koeln] 13 00 30 00 457 [Desreeldworf] 5 00 52 00 549 [Desreeldworf] 42 00 58 00 549 [Destend] 42 00 58 00 549 [Destend] 42 00 50 00 251 [Heanster] eed (location) hegin (ed]last) 1 5 1 1 5 3 1 5 4 1 3 4 1 3</pre>	
OK	

Figure 4.5: The same input file as in Figure 4.3 in the number-format.

View Graph	
<pre>begin (Lolagraph) Begin (Location) [2.1] 30 955 [Acela] 30 557 [Decemediant] 30 540 Decemend 30 610 Decemend] 30 610 Decemend] 30 321 [Manuter] med (Locations) begin (adjlast) 1 2 1 1 5 3 2 3 1 2 4 1 3 4 1 3 6 2 4 5 1 4 6 2 4 5 1 4 6 2 5 6 1 5 6 2 4 6 9 5 6 1 8 6 2 5 6 1 8 6 1</pre>	A.
OK	

Figure 4.6: The input data of Figure 4.3 in the no-coordinate format.

4.7 File Type sol (containing solution data)

The information about the solution of a location problem is saved in files of type *sol*. Depending on the type of problem solved, this file may contain different information. In the first environment *class* the classification string of the solved problem is given. In the environment "objective value" the optimal objective value is specified whereas in the environment "polygonlist" one (or several, as e.g. in case of multicriteria problems) sets of optimal points/polyhedrons can be given.

```
begin {class}
classification
end {class} begin {result}
begin {objective value}
z z z
end {objective value}
begin {polygonlist}
begin {polygon}
x_1 \, y_1
x_2 y_2
÷
x_n y_n
end {polygon}
begin {polygon}
x_1 \ y_1
x_2 \, y_2
:
x_n y_n
end {polygon}
end {polygonlist}
end {result}
```

Example In the following the input data and the solution file are given for a planar location problem of type $1/P/./l_{\infty}/\sum$.

```
begin {location} [2,1]
2 2 1 [OrtA]
5 3 1 [OrtB]
8 3 1 [OrtC]
4 4 1 [OrtD]
end {location}
begin {class}
$1/P/./l_{\infty}/\sum$
end {class}
begin {result}
```

```
begin {objective value}
7
end {objective value}
begin {polygonlist}
begin {polygon}
5 3
4 4
end {polygon}
end {polygonlist}
end {result}
```

Chapter 5

Writing a LOLA Application

In the following we will explain briefly how the LOLA-libraries can be used directly in a C++ program without using the LOLA frontend. We describe the components of a C++ program using LOLA to solve a planar minisum problem with squared Euclidean distance and restrictions.

First we have to include the definitions of the routines we need. In our case we need the routines that handle location files (read, write) and the algorithms for planar problems.

```
#include <LOLA/facs_util.h>
#include <LOLA/planealg.h>
```

Next we have to define some variables to store the objective value, the name of the location file (e.g. .../LOLA/examples/prog/test.loc), etc.

```
main() {
  double objval[2];
  string normact;
  string locfile="test.loc";
  string extrafile="test.restr";
  facs_util EX;
  planealg A;
  restrictions Restr;
```

Now we read the data for the problem.

ifstream file (locfile,ios::in); EX.ReadLoc(file); All necessary data is available to solve the corresponding unrestriced problem, which is done in the next step. Also the optimal solution is printed and the solution is shown graphically.

```
objval[0] = A.12sqr_sum(EX);
A.WriteOpt();
list<location> AlgSol = A.alg_solution();
normact = "12sqr";
EX.View(objval[0],normact,AlgSol,Restr);
```

Next we read in addition a restriction file and solve the corresponding restricted problem.

```
ifstream filerestr (extrafile,ios::in);
Restr = ReadRestr(filerestr);
objval[1] = A.12sqr_sum(EX,Restr);
A.WriteOpt();
```

Finally, we show again the data, the restriction and the solution graphically in a window.

```
AlgSol = A.alg_solution();
EX.View(objval[1],normact,AlgSol,Restr);
```

The resulting complete C++ file given in the following can be compiled after LOLA is installed.

```
ifstream file (locfile,ios::in);
EX.ReadLoc(file);
* solve problem 1/P/./l2**2/sum
objval[0] = A.l2sqr_sum(EX);
A.WriteOpt();
list<location> AlgSol = A.alg_solution();
normact = "l2sqr";
EX.View(objval[0],normact,AlgSol,Restr);
* read restriction-file
ifstream filerestr (extrafile,ios::in);
Restr = ReadRestr(filerestr);
* solve problem 1/P/R/12**2/sum
                         *
objval[1] = A.l2sqr_sum(EX,Restr);
A.WriteOpt();
* Output in a LEDA-Window
AlgSol = A.alg_solution();
EX.View(objval[1],normact,AlgSol,Restr);
}
```

The file "test.cpp" containing this C++ code can be found in the directory $\dots/LOLA/examples/prog$, where also a makefile is provided.

At the end of this section we show how some of the C++ methods used above are defined.

```
double planealg::l2sqr_sum(facilities& EX)
{
    double result;
```

```
result = EX.l2sqr_sum();
solution = EX.alg_solution();
return result;
}
double planealg::l2sqr_sum(facilities& EX, restrictions& R)
{
    double result;
    result = R.l2sqr_sum(EX);
    solution = R.alg_solution();
    return result;
}
```

Chapter 6

A Classification Scheme for Location Problems

In this chapter we describe the classification scheme for location problems used in the frontend of LOLA. A detailed description of this scheme can be found in Hamacher and Nickel¹.

The classification scheme has five positions:

Pos1/Pos2/Pos3/Pos4/Pos5.

The meaning of each position is described in the following.

Pos1 This position contains information about the number and the type of the new facilities.

- **Pos2** The type of the location problem with respect to the decision space. This entry should e.g. differentiate between continuous, network and discrete problems.
- **Pos3** In this position is room for describing particularities of the specific location problem. For example, information about the feasible solutions or about capacity restrictions can be included in this position.
- **Pos4** This position is devoted to the relation of new and existing facilities. This relation may be expressed by some distance function or simply by assigned costs.

Pos5 The last position contains a description of the objective function.

If we do not make any special assumptions in a position this is indicated by /./. For example, /./ in Position 5 means that we consider any objective function and /./ in Position 3 means that the standard assumptions for the problem described in the remaining four positions hold. For example in planar location problems /./ in Position 3 implies e.g. that

¹H.W. Hamacher and S. Nickel: "Classification of Location Models". Technical Report in Wirtschaftsmathematik No. 19, Universität Kaiserslautern, Department of Mathematics, 1996. To appear in *Location Science*.

we have (as usual) positive weights for the existing facilities. In general we also assume by default that the objective function is to be minimized.

Position	Meaning	Usage (Examples)
1	number of new facilities	
2	type of problem	 P planar location problem D discrete location problem G location problem on a network
3	specials	$w_m = 1$ all weights are equal \mathcal{R} or R a forbidden region
4	type of distance function	$egin{array}{ccc} l_1 & { m Manhattan\ metric} \ \gamma & { m a\ gauge} \ d(V,V) & { m node\ to\ node\ distance} \ d(V,G) & { m node\ to\ points\ of\ graph\ distance} \end{array}$
5	type of objective function	\sum Median problem max Center problem $Q - \sum$ Multicriteria (Pareto) median problem

The following table gives an overview about the usage of the classification scheme.

Note that, due to font limitations, in the LOLA frontend some symbols may not look exactly like they do in this manual.

A list of possible symbols used in each position of the classification scheme is given in the following table.

Position 1	Position 2	Position 3	Position 4	Position 5
$n \in \{1, \ldots, N\}$	\mathbb{R}^{d}	\mathcal{R}	l_p	\sum
l	Р	\mathcal{F}	γ	max
p	Н	B	γ_{pol}	CD
A	G	$w_m = 1$	γ_{mix}	\int_{d}
C	\mathcal{G}_D	$w_m \neq 0$	·	$\int \int d_1 d_2$
R	\mathcal{T}	w_m : distribution	d_{Haus}	$Q - \sum_{par}$
T	D	w_m : RV	d_{inhom}	$Q - \sum_{lex}$
G		w_m : $f(\cdot)$	$d(\mathcal{V},\mathcal{V})$	$Q - \sum_{MO}$
#		mc	$d(\mathcal{V},\mathcal{G})$	$Q - (\sum, \max)_{par}$
#,#		alloc	$d(\mathcal{V},\mathcal{T})$	\sum_{comp}
		cap	$d(\mathcal{G},\mathcal{V})$	\sum_{uncov}
		bdg	$d(\mathcal{T},\mathcal{V})$	$\sum_{cov} + \sum_{uncov}$
		d_{max}	$d(\mathcal{G},\mathcal{G})$	\sum_{cov}
		price	$d(\mathcal{T},\mathcal{T})$	QAP
		queue		\sum_{ord}
				\sum_{prob}
				\max_{prob}
				\sum_{hub}
				φ : property

Chapter 7

The Components of LOLA

7.1 GUI – Graphical User Interface

The GUI is based on the 5-position classification scheme for facility location problems introduced in Chapter 6 to easily specify the type of problem which is going to be solved by LOLA.

If TCL/TK is available on your system, calling LOLA creates the window depicted in Figure 2.1.

According to the classification scheme, the menu of the GUI contains buttons for

Number to select the number of new facilities - in case of N-facility problems with the Insert-number-window as shown in Figure 7.1.

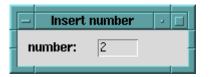


Figure 7.1: Insert-number-window

Type to select the basic type (P,G,D,T) of the problem.

- P: planar problems
- G: graph problems
- D: discrete problems
- T: tree problems

Specials to select special assumptions for the set of solutions, which may be

- equal weights In case of equal weights, faster procedures are available for some types of location problems.
- restrictions With the option outside we can choose whether the forbidden zone is inside or outside the given restrictions. The restrictions can be:
 - polyhedron The restriction file must describe a (possibly non-convex) polyhedron.
 - conpolyhedron The restriction file must describe a convex polyhedron.
 - circle The restriction file must describe a circle.
 - rectangle The restriction file must describe a rectangle.
 - all The restriction file must describe one or more of the above four possibilities in arbitrary order and number.

barriers Not implemented yet!

none Default possibility : no restrictions in the problem

Metric to select the distance function. The options are

- 11 The l_1 -norm is chosen.
- 12 The l_2 -norm is chosen.
- $|l2^{**}2|$ The l_2^2 -norm is chosen.
- linf The l_{∞} -norm is chosen.
- lp The l_p -norm is chosen, where p can be selected in Options under Preferences
- gauge The distance measure is a self-created gauge.
- block The distance measure is a block norm.

For Graph and Tree-algorithms we have the options

- d(V,V) The optimal points are searched only on nodes.
- d(V,G) The optimal points are searched on the entire graph.
- d(V,T) The optimal points are searched on the entire graph which is a tree.
- Objective to select the type of objective function. The options are

median if the sum of (weighted) distances should be minimized.

center if the maximum (weighted) distance should be minimized.

Q-median if the sum over all distances should be minimized with respect to more than one criterion (i.e. the dimension of the weights is bigger than 1).

Q-center if the maximum (weighted) distance should be minimized with respect to more than one criterion (i.e. the dimension of the weights is bigger than 1).

Furthermore the GUI contains

File • to select files providing data for given problems, e.g. Load Location

- to view this data, e.g. View Location (**Remark:** This option is not to edit a file) or
- to create new data files, e.g. Graphical Edit and Create Example

Help to call the online help-browser,

Options to set general preferences on the maximum number of iterations, default metric for l_p or other problem dependent settings.

The solution process of the classified problems can be started by clicking on the button Computation.

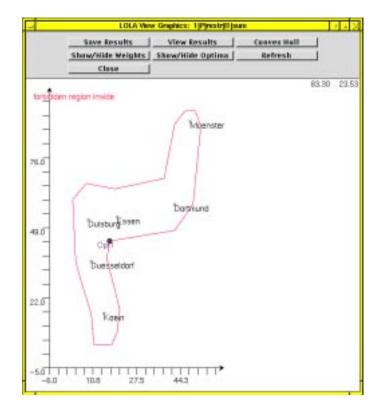


Figure 7.2: Solution window with a non-convex polyhedral restriction

A solution window (e.g. as shown Figure 7.2) could contain the following options:

Save Results to save the current solution,

View Results to view the results in numeric format,

Refresh to redraw the solution window,

Close to close the window.

Solution windows for planar problems additionally contain the buttons

Convex Hull to draw, respectively remove the convex hull of the set of existing facilities,

Weights to show, respectively hide the weights of the existing facilities,

View Gauge to view the unit ball of a special gauge (appears only if the metric is set to gauge or block).

In solution windows for network problems the following buttons are available.

Node_Weights to show, respectively hide the weights of the edges of the network,

Edge_Weights to show, respectively hide the weights of the nodes of the network.

For discrete problems the following buttons are additionally available in the solution window.

Fix Costs to show, respectively hide the fix costs for the supply points,

Weights to show, respectively hide the weights of the demand points,

View Cost Matrix to view the cost matrix (advisable only for small problems).

7.2 Text Based Version of LOLA

All algorithms of LOLA can also be adressed using command-line options in the *text based* mode. TCL/TK is not needed for the text-based mode. The necessary input to solve a location problem can be given. Upon invocation LOLA returns the solution in text or graphical format, however the latter can be completely suppressed, rendering LOLA capable of operating text-only. This mode of operation is well suited to perform automated or repeated tasks.

The text-based mode is automatically entered if command-line options are detected and it is the only available mode if LOLA has been configured with --withtcltk=no. Figure 7.3 shows the available options.

The single-hyphen options detail which task LOLA is to perform, whereas --output specifies how to present the solution. The option --output allows a comma-seperated list of arguments, which are parsed from left to right:

```
lola - a < algorithm > [-1|-r|-g|-d|-m < file >] [-p < n >] [-n < n >] [--output = < arguments >]
```

Options:

```
-a : the algorithm, which is to be performed on the data (see below)
-l : <file> contains the existing facilities
-r : <file> contains restrictions
-g : <file> contains a (directed or undirected) graph
-d : <file> contains polygonal gauge definitions
-m : <file> contains a cost matrix for n-facility problems
-p : <n> is the exponent for an l<sub>p</sub>-norm
-n : <n> is the number of new facilities for problems on graphs
--output:
    this option takes a comma-seperated list of arguments:
        [no]windowed : [dont] present the solution graphically
        [file=]<file>: write solution as text into <file>
        only the rightmost argument of each type takes effect
```

Figure 7.3:	Command	line	options	of	$_{\mathrm{the}}$	$\operatorname{text-based}$	version	of	LOLA
-------------	---------	------	---------	----	-------------------	-----------------------------	---------	----	------

nooutput	The solution is presented graphically in a
	window and text-based on standard output.
output=prob1.sol	The solution is saved in the file prob1.sol
output=nowindowed	No windows pop up – this enforces a
	text-only operation
output=file1,file=windowed	The solution is saved into the file windowed,
	since the second argument supercedes the
	first. A solution window is generated.

	-					_	
-a <algorithm></algorithm>	-1	-m	-r	-p	-g	-d	-n
l1_max, l2_max, linf_max,	Х						
l1_v1_max, linf_v1_max, l2sqr_qsum	Х						
l1_sum, l2_sum, l2sqr_sum, linf_sum	Х						
11_2sum, linf_2sum	Х						
lp_sum	Х		0	Х			
in_l1_sum, out_l1_sum, in_l2sqr_sum,	Х		Х				
out_l2sqr_sum, in_linf_sum,	Х		Х				
<pre>out_linf_sum, in_convPoly_v1_l2_max,</pre>	Х		Х				
in_convex_linf_max, in_convex_l1_max	Х		Х				
barr_12_sum	Х		Х				
N_l1_sum_v1, N_l2sqr_sum, N_l2_sum_v1,	Х	Х					
N_linf_sum_v1, N_l1_max, N_linf_max	Х	Х					
dir_median, undir_median,					Х		
abs_undir_median					Х		
abs_tree_median, abs_undir_center,					Х		
abs_dir_center,loc_tree_center,					Х		
abs_tree_center,loc_tree_median,					Х		
loc_dir_center,loc_undir_center					Х		
N_median_cplex, N_median_partitioning,					Х		Х
N_median_exchange, N_median_greedy,					Х		Х
N_center_partitioning, N_center_greedy					Х		Х
medPareto, loc_medPareto, loc_cenPareto,					Х		
dir_medPareto, dir_locmedPareto,					Х		
dir_loc_cenPareto, dir_cenPareto					Х		
medLexi, loc_medLexi, loc_cenLexi,					Х		
dir_medLexi, dir_loc_medLexi,					Х		
dir_loc_cenLexi					Х		
gauge_median, bi_crit_gauge_median	Х					Х	
gauge_center	Х					Х	
L_l1_sum_M3, L_linf_sum_M3,	Х						
L_12_sum_M3, L_12_sum_M2logM,	X						
L_12_sum_M2,	X						
L_lp_sum_M3, L_lp_max_M4	X			Х			
L_l1_max_M4, L_linf_max_M4,	X						
L_12_max_M4, L_12_max_MlogM,	X						
L_12_max_M2logM,	X						
L_block_sum_M3, L_block_max_M3	X					X	
L_RkonvPoly_12_sum, L_RkonvPoly_11_sum,	X		Х			1	
L_RkonvPoly_lp_sum,	X		X	Х			
L.RkonvPoly_linf_sum,	X		X	1			
L_RkonvPoly_llock_sum	Х		Х			Х	
Table 7.1: Easible combinations of	Λ	<u> </u>	A line	<u> </u>		Λ	

Table 7.1: Feasible combinations of command-line options

argument of -a	problem class	LOLA method
l1_sum	$1/P/./l_1/\Sigma$	planealg::11_sum
in_l1_sum	$1/P/R/l_1/\sum$	planealg::l1_sum
out_11_sum	$1/P/R^c/l_1/\sum$	planealg::l1_sum
N_11_sum_v1	$N/P/./l_1/\sum$	planealg::N_l1_sum
11_2sum	$1/P/./l_1/2 - \sum$	planealg::11_2sum
L_11_sum_M3	$\frac{1}{1L/P} \frac{1}{2}$	planealg::L_l1_sum_M3
L_RkonvPoly_11_sum	$1L/P/R = convpolyhed/l_1/\sum$	planealg::L_RkonvPoly_11_sum
12_sum	$\frac{12/1/n}{1/P/./l_2/\Sigma}$	planealg::12_sum
barr_12_sum	$1/P/B/l_2/\sum$	planealg::12_sum
N_12_sum_v1	$N/P/./l_2/\sum$	planealg::N_12_sum_v1
L_12_sum_M2logM	$\frac{11/1/1/2}{1L/P/./l_2/\Sigma}$	planealg::Ll2_sum_M2logM
L_12_sum_M3		planealg::L_l2_sum_M3
L_12_sum_M2	$1L/P/w_i = 1/l_2/\sum$	planealg::L_l2_sum_M2
L_RkonvPoly_12_sum	$\frac{1L/P}{R} = convpolyhed/l_2/\sum$	planealg::L_RkonvPoly_12_sum
12sqr_sum	$\frac{12/1/n}{1/P/./l_2^2/\sum}$	planealg::l2sqr_sum
in_12sqr_sum	$\frac{1}{1/P/R/l_2^2}$	planealg::12sqr_sum
out_12sqr_sum	$\frac{1}{1/P/R^{c}/l_{2}^{2}}/\sum_{1/P/R^{c}/l_{2}^{2}}$	planealg::12sqr_sum
_	$N/P/./l_2^2/\sum$	planealg::N_l2sqr_sum
N_12sqr_sum 12sqr_qsum		
	$\frac{1/P/./l_2^2/Q - \sum}{1/P/./l_p/\sum}$	planealg::l2sqr_qsum
lp_sum		planealg::lp_sum
lp_sum	$1/P/R = convpolyhed/l_p/\sum_{N/P/l_p/l_p}$	planealg::lp_sum
N_lp_sum_v1	$N/P/./l_p/\sum_{l=1,l_p/l_p/l_p}$	planealg::N_lp_sum_v1
L_lp_sum_M3	$1L/P/./l_p/\sum_{l=1,l\neq p/p}$	planealg::Llp_sum_M3
L_RkonvPoly_lp_sum	$1L/P/R = convpolyhed/l_p/\sum$	planealg::L.RkonvPoly_lp_sum
linf_sum	$1/P/./l_{\infty}/\sum_{1/P/P/l_{\infty}}$	planealg::linf_sum
in_linf_sum	$1/P/R/l_{\infty}/\sum_{l_{\infty}}$	planealg::linf_sum
out_linf_sum	$1/P/R^c/l_{\infty}/\sum_{N/D}$	planealg::linf_sum
N_linf_sum_v1	$N/P/./l_{\infty}/\sum$	planealg::N_linf_sum
linf_2sum	$1/P/./l_{\infty}/2 - \sum$	planealg::linf_2sum
L_linf_sum_M3	$1L/P/./l_{\infty}/\sum$	planealg::L_linf_sum_M3
L_RkonvPoly_linf_sum	$1L/P/R = convpolyhed/l_{\infty}/\sum$	planealg::L_RkonvPoly_linf_sum
gauge_median	$1/P/./\gamma/\sum$	gaugealg::sum
bi_crit_gauge_median	$1/P/./\gamma/2 - \sum_{par}$	gaugealg::bi_crit_sum
L_block_sum_M3	$1L/P/./\gamma_B/\sum$	gaugealg::L_block_sum_M3
L_RkonvPoly_block_sum	$1L/P/R = convpolyhed/\gamma_B/\sum$	gaugealg::L_RkonvPoly_block_sum
l1_max	$1/P/./l_1/max$	planealg::l1_max
l1_v1_max	$1/P/w_i = 1/l_1/max$	planealg::l1_v1_max
in_convex_11_max	$1/P/R = convex/l_1/max$	planealg::l1_max
N_11_max	$N/P/./l_1/max$	planealg::N_l1_max
L_11_max_M4	$1L/P/./l_1/max$	planealg::L_l1_max_M4
12_max	$1/P/./l_2/max$	planealg::elzhearn
in_12_max	$1/P/R/l_2/max$	planealg::12_max
L_12_max_M4	$1L/P/./l_2/max$	planealg::L_12_max_M4
L_12_max_MlogM	$1L/P/./l_2/max$	planealg::Ll2_max_MlogM
L_12_max_M2logM	$1L/P/./l_2/max$	planealg::Ll2_max_M2logM

L_lp_max_M4	$1L/P/./l_p/max$	planealg::Llp_max_M4
linf_max	$1/P/./l_{\infty}/max$	planealg::linf_max
linf_v1_max	$1/P/v_i = 1/l_{\infty}/max$	planealg::linf_v1_max
in_convex_linf_max	$1/P/R = convex/l_{\infty}/max$	planealg::linf_max
N_linf_max	$N/P/./l_{\infty}/max$	planealg::N_linf_max
L_linf_max_M4	$1L/P/./l_{\infty}/max$	planealg::L_linf_max_M4
gauge_center	$1/P/./\gamma/\max$	gaugealg::max
L_block_max_M3	$1L/P/./\gamma_B/\max$	gaugealg::L_block_max_M3

Table 7.2: Planar algorithms of text-based LOLA

argument of -a	problem class	LOLA method
dir_median	$1/G_D/./d(V,V)/\sum$	lgraphalg::median
undir_median	$1/G/./d(V,V)/\sum$	lgraphalg::median
abs_undir_median	$1/G/./d(V,G)/\sum$	lgraphalg::abs_median
loc_tree_median	$1/T/./d(V,V)/\sum$	lgraphalg::loc_tree_median
abs_tree_median	$1/T/./d(V,T)/\sum$	lgraphalg::abs_tree_median
medPareto	$1/G/./d(V,G)/2 - \sum -par$	lgraphalg::medPareto_bi
	$1/G/./d(V,G)/Q - \sum -par$	lgraphalg::medPareto_Q
loc_medPareto	$1/G/./d(V,V)/Q - \sum -par$	lgraphalg::loc_medPareto
dir_medPareto	$1/G_D/./d(V,G)/Q - \sum -par$	lgraphalg::medPareto
dir_loc_medPareto	$1/G_D/./d(V,V)/Q - \sum -par$	lgraphalg::loc_medPareto
medLexi	$1/G/./d(V,G)/Q - \sum -lex$	lgraphalg::medLexi
loc_medLexi	$1/G/./d(V,V)/Q - \sum -lex$	lgraphalg::loc_medLexi
dir_medLexi	$1/G/./d(V,G)/Q - \sum -lex$	lgraphalg::medLexi
dir_loc_medLexi	$1/G/./d(V,V)/Q - \sum -lex$	lgraphalg::loc_medLexi
abs_dir_center	$1/G_D/./d(V,G)/\max$	lgraphalg::abs_center
loc_dir_center	$1/G_D/./d(V,V)/\max$	lgraphalg::center
loc_undir_center	$1/G/./d(V,V)/\max$	lgraphalg::center
abs_undir_center	$1/G/./d(V,G)/\max$	lgraphalg::abs_center
loc_tree_center	$1/T/./d(V,V)/\max$	lgraphalg::loc_tree_center
abs_tree_center	$1/T/./d(V,T)/\max$	lgraphalg::abs_tree_center
loc_cenPareto	$1/G/./d(V,V)/\max$	lgraphalg::loc_cenPareto
dir_loc_cenPareto	$1/G_D/./d(V,V)/\max$	lgraphalg::loc_cenPareto
dir_cenPareto	$1/G_D/./d(V,G)/\max$	lgraphalg::cenPareto
loc_cenLexi	$1/G/./d(V,V)/Q - \max - lex$	lgraphalg::loc_cenLexi
dir_loc_cenLexi	$1/G/./d(V,V)/Q - \max - lex$	lgraphalg::loc_medLexi
N_median_cplex	$N/G/./d(V,V)/\sum$	lgraphalg::N_median_cplex
N_median_partitioning	$N/G/./d(V,V)/\sum$	lgraphalg::N_median_partitionin
N_median_exchange	$N/G/./d(V,V)/\sum$	lgraphalg::N_median_exchange
N_median_greedy	$N/G/./d(V,V)/\sum$	lgraphalg::N_median_greedy
N_center_partitioning	$N/G/./d(V,V)/\max$	lgraphalg::N_center_partitionin

N_center_greedy
$$N/G/./d(V,V)/\max$$
 |graphalg::N_center_greedy
Table 7.3: Graph algorithms of text-based LOLA

Each algorithm of LOLA has been assigned a short, descriptive name which is the argument to the -a option. The choice of an algorithm determines the type of input files needed for the solution of the location problem. Table 7.1 on page 40 lists all feasible algorithm/data combinations, where "X" means *mandatory* and "O" means *optional*. Tables 7.2 and 7.3 show which class of location problems is solved by each algorithm and which LOLA-class method is used.

Examples A command could be

lola -lmydata.loc -al1_sum for a 1-location problem which has to be solved with respect to the l_1 norm and as a median problem.

or *lola -lmydata2.loc -aN_l1_max -mmat.1* for a N-location problem which has to be solved with respect to the l_1 norm and as a center problem.

7.3 Graphical Editor

This graphical editor enables the user to generate input for LOLA. The user can use the mouse to create a problem file for a location or a network problem. It will create a location file, a graph file, a gauge file or a restriction file in the correct input format. The menubar allows the user to choose File, Options or Help.

7.3.1 File

Under the File menu the following options are available.

New to clear the window.

Load to load a location or a restriction file (must have correct input format).

Load Interactionmatrix to load a matrix file for an N-location problem.

Save Location to save the coordinates and weights of locations.

Save Graph to save the coordinates and weights of nodes and edges.

Save Restriction to save the coordinates of restrictions.

Save Interactionmatrix to save a matrix file (available for number > 1).

Print to print the input as a postscript.

Quit to quit the Grapheditor and go back to LOLA.

7.3.2 Options

NewMax to change the xmax and ymax for the input window (default value is 50 and integer).

Draw Hull to draw the convex hull for all locations.

<u>Number</u> to insert the number of new locations. The user is able to insert the interdependence-matrix (default value is 1).

Locations

- clicking on the left mouse button defines an existing facility at the actual position.
- with pressed Shift-Key, clicking on the left mouse button on an existing point gives a dialog to change the weight of this point (default value is 1).
- with pressed Control-Key, clicking on the left mouse button on an existing point deletes this point.
- clicking on the right mouse button and moving the mouse moves the point until the mouse button is released.
- with pressed Shift-Key, clicking on the right mouse button on an existing point gives a dialog to insert a string as a description for this location.

<u>Restrictions</u> choose <u>outside</u> and the forbidden region is outside the restriction, otherwise the forbidden region is inside (default) and then choose one of the following restrictions.

Polyhedron

- clicking on the left mouse button defines a point of the polyhedron.
- double clicking on the left mouse button defines the last point of this polyhedron.
- with pressed Control-Key, clicking on the left mouse button on an existing point deletes all polyhedra.
- clicking on the right mouse button and moving the mouse moves the polyhedron until the mouse button is released.

Convex Polyhedron

- clicking on the left mouse button defines a point of the polyhedron.
- double clicking on the left mouse button defines the last point of this convex polyhedron and creates a convex polyhedron.
- with pressed Control-Key, clicking on the left mouse button on an existing point deletes all convex polyhedra.

Circle

• clicking on the left mouse button defines the middle- point of the circle.

- with pressed Shift-Key, clicking on the left mouse button and moving the mouse creates the circle and defines the radius if the mouse button is released.
- with pressed Control-Key, clicking on the left mouse button on an existing middlepoint deletes the circle.
- clicking on the right mouse button and moving the mouse moves the circle until the mouse button is released.

Rectangle

- clicking on the left mouse button defines the point on the left bottom of the rectangle.
- with pressed Shift-Key, clicking on the left mouse button and moving the mouse creates the rectangle and defines the sides a and b. If the mouse button is released then an angle α can be inserted to rotate the rectangle (-90 < α <90).
- with pressed Control-Key, clicking on the left mouse button on an existing point deletes the rectangle.
- clicking on the right mouse button and moving the mouse moves the rectangle until the mouse button is released.

Gauge to choose the maximal extension of the gauge and to create gauges with the buttons:

- Save Gauge to save single gauge in a file.
- Show/Hide Unit Ball to make the unit ball of the gauge (in)visible.
- Clear to clear the input window.
- Append to Gauge-List to append the actual gauge to a polygauge list (if no such list exists, a new one is opened).
- Save Gauge-List to save the whole polygauge list in a file.
- Clear Gauge-List to delete the existing polygauge list.
- Symmetr/Unsymmetr to create symmetrical or unsymmetrical polygauges (default is symmetrical: Only one of two symmetrical extreme points of the unit ball has to be added, the other one is added automatically).
- Refresh to refresh the input window.
- Close to close the input window.

Undirected Graph to choose whether the graph is a directed one or an undirected one.

- to draw an edge click with the middle mouse button (assuming the mouse has three buttons) on one location and release the button on another location.
- in case the mouse has two buttons only, the user can use the Alt-Key together with the left mouse button to draw edges.
- to insert an edge-weight press the Shift-Key and click on the left mouse button.
- to delete an edge press the Control-Key and click on the left mouse button.

In the bottom appear the actual coordinates of the mouseposition and the actual insert Mode.

7.4 Other Software Used by LOLA

Tools and utilities which are used:

- LEDA,
- TCL/TK,
- CPLEX, or some other type of LP–solver, which is able to process files in the MPS-Format

The implementation language is C/C++.

Chapter 8

System Design

The system consists of the three main classes *planealg* (P), *graphalg* (G) and *discalg* (D). Through these classes all routines in the library can be called and controlled.

8.1 System Structure

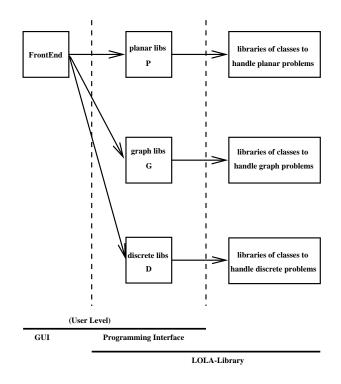
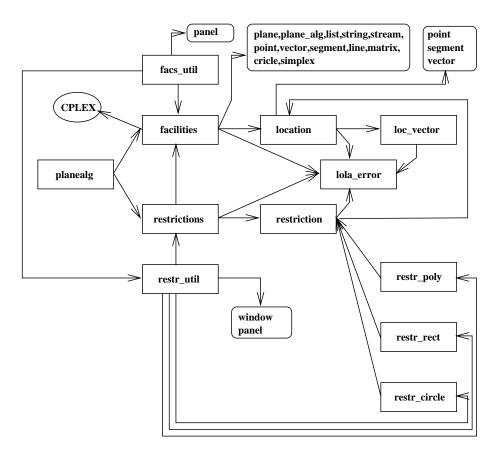


Figure 8.1: System Structure. The layers of the user-interfaces and the libraries are shown. The internal design of the libraries for handling the three types of location problems is specified in the text.



8.2 Component Structure Type P

Figure 8.2: Component Structure P. The arrows stand for "uses/accesses"-relations between the modules. Components of LOLA are represented by rectangles, components of LEDA are represented by smooth rectangles, and other components are represented by ellipsoids.

This is the graphical representation of the inner structure of the Type P–libraries of LOLA. All dependencies and accesses to LEDA and other pre–requisites are shown in this figure. Furthermore the coupling of this part of the system is described by the arrows.

8.3 Library Inclusions Type P

Figure 8.3 shows the LOLA classes and the corresponding libraries in which they are located. The structure provides a separation of unrestricted problems (libLp), restricted problems (libLpr) and utility functions (libLpu).

If an executable program is statically linked with the LOLA libraries, the library sequence has to be libLpu, libLpr, libLp.

Example (with GNU's C++):

g++ -o myprog myprog.o -lotherlibs -lLpu -lLpr -lLp -lotherlibs

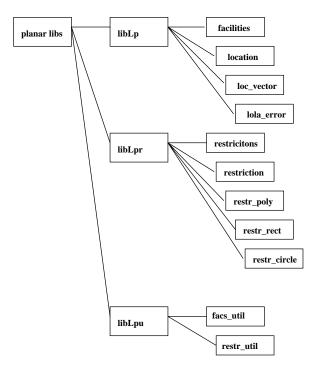


Figure 8.3: Library Structure P. Showing the inclusions of classes to libraries.

This will produce the statically linked executable file myprog. For more information about the linker see your GNU C/C++ manual or your system's C/C++ compiler manual.

Part II

The LOLA Libraries

Chapter 9

Unrestricted Planar Classes

9.1 Real-Valued Location-Vectors (Loc_Vector)

1. Definition

An instance of the data type Loc_Vector consists of an n-dimensional array of reals.

2. Creation

Loc_Vector $V(int \ dim = 0);$

creates a *dim*-dimensional *Loc_Vector*, default dimension is 0.

 $Loc_Vector V(double dim, ...);$

creates an instance *Loc_Vector* with the following initialization: $v(dim, arg_1, ..., arg_{dim})$. All numbers must be doubles.

3. Operations

Loc_Vector	V + &v1	returns the sum of V and $v1$.
Loc_Vector	V – & $v1$	returns the result of the subtraction of $v1$ from V .
$Loc_Vector\&$	V + = &v1	adds $v1$ to V .
$Loc_Vector\&$	V -=&v1	subtracts $v1$ from V .
$Loc_Vector\&$	$V *= double \ scalar$	multiplies V by <i>scalar</i> .

$Loc_Vector\&$	V += double scalar	adds $scalar$ to V .
$Loc_Vector\&$	V $-=$ double scalar	subtracts $scalar$ from V .
$Loc_Vector\&$	V /= double scalar	divides V by <i>scalar</i> .
Loc_Vector	$V \ * \ double \ scalar$	returns the product of V and $scalar$.
Loc_Vector	V + double scalar	returns the sum of V and <i>scalar</i> .
Loc_Vector	$V\ -\ double\ scalar$	returns the result of the subtraction of $scalar$ from V .
Loc_Vector	$V \hspace{0.1 in}/ \hspace{0.1 in} double \hspace{0.1 in} scalar$	returns the result of the division of V by $scalar$.
double	$V * V_2$	inner product of V with V_2 .
double&	V ~[int~idx]	returns a reference to the idx -th component of V .
bool	V < &v1	returns true if $V < v1$ for all elements.
bool	$V \ll \&v1$	returns true if $V \leq v1$ for all elements.
bool	V > &v1	returns true if $V > v1$ for all elements.
bool	V >= &v1	returns true if $V \ge v1$ for all elements.
bool	V != &v1	returns true if $V \neq v1$ for all elements.
bool	V == &v1	returns true if $V = v1$ for all elements.
Loc_Vector&	$V = V_2$	assignment operator.
double	$V.norm(int \ p)$	returns the p -norm (p -metric) of V .
void	$V.\mathrm{abs}()$	returns the absolute value of V .
int	$V.{ m size}()$	returns the dimension of V .
bool	$V.\mathrm{null_chk}()$	returns true if one or more components of V are zero.
Loc_Vector	$V.rotate(double \ phi)$	rotates V by phi .

ostream& << (ostream & stream, Loc_Vector & v)

writes V componentwise.

4. Implementation

All operations on a Loc_Vector take time O(size()).

9.2 Real-Valued Locations with weights (location)

1. Definition

An instance of the data type *location* consists of two Loc_Vectors.

2. Creation

location L(int dim = 2, int wht = 1);

creates a location with a *dim*-dimensional *Loc_Vector* for the coordinates and a *wht*-dimensional *Loc_Vector* for the weights.

location L(double dim, ...);

creates an instance *Location* with the following initialization: v(dimension, #weights, coord1, coord2, ..., wht1, wht2, ...). All numbers must be doubles.

3. Operations

double	L.norm(int p)	returns the p -norm (p -metric) of L .
int	$L.\mathrm{dim}()$	returns the dimension of L .
int	$L.wht_dim()$	returns the number of weights of L .
int	L.overall()	returns $dim() + wht_dim()$ of L.
Loc_Vector&	$L.\mathrm{pos}()$	returns a reference to the coordinate Loc_Vector .
Loc_Vector&	L.wht()	returns a reference to the weights Loc_Vector .
void	$L.\mathrm{transform}()$	transforms the coordinates. Precondition: $L.dim() = 2.$

void	L.retransform()	retransforms the coordinates. Precondition: $L.dim() = 2.$
double	$L.r_angle(location \&L1)$	calculates the radian angle between L and $L1$.
double	L.d.angle(location &L1)	calculates the degree angle between L and $L1$.
point	$L.\mathrm{loc2point}()$	transforms location L into type point. Precondition : $dim() = 2$.
vector	$L.\mathrm{loc2vector}()$	transforms location L into type vector (not Loc_Vector). Precondition : $dim() > 0$.
segment	L.makesegment(location L1)	returns a segment built of location L and $L1$. Precondition : $L.dim() = 2$.
double&	L [int i]	returns a reference to the i -th coordinate of L .
double&	$L \ (\ int \ j)$	returns a reference to the j -th weight of L .
double	L * &L1	returns product of L and $L1$.
location	L * double &scalar	returns product of L with <i>scalar</i> .
location	L / double &scalar	returns the result of the division of L by <i>scalar</i> .
location	L + &L1	returns $location$ which coordinates are the sum of of the $L1$ -coordinates and the L -coordinates.
location	L - &L1	returns <i>location</i> which coordinates are the dif- ference of of the $L1$ -coordinates and the L - coordinates.
int	L == &L1	tests for equality in coordinates and weights of L and $L1$ (true = 1, false = 0).
int	L != &L1	tests for inequality in coordinates and weights of L and $L1$ (true = 1, false = 0).
location&	L=(location &L1)	assignment operator.

9.3 Line (Line)

1. Definition

An instance of the data type *Line* consists of three doubles and the line-defining locations; (ax + by - c = 0).

2. Creation

Line V;

creates a zero-Line.

Line $V(location \ l1, \ location \ l2);$

creates a *line* defined by l1 and l2.

3. Operations

Line&	V = &L	assignment operator.
double&	V.m()	returns a reference to the slope M of V .
location&	V.L1()	returns a reference to the first defining location $L1$.
location&	V.L2()	returns a reference to the first defining location $L2$.
double&	$V.\mathrm{a}()$	returns a reference to the x -coefficient of V .
double&	$V.\mathrm{b}()$	returns a reference to the y -coefficient of V .
double&	V.c()	returns a reference to the constant c .
bool	V.parallel($Line & L$)	returns true if the lines V and L are parallel; otherwise false.
double	$V.weighted_distance(location \& L)$	
		calculates the weighted euclidean distance from L to the line V .
double	V.distance(location &L)	calculates the unweighted euclidean distance from L to the line V .
double	$V.lp_distance(location \&L, int p)$	

calculates the unweighted l_p -distance from L to the line V.

location	V. intersection (Line & L)	calculates the intersection-location of the two lines.
bool	V < &L	returns true if L is parallel to V and lies below V .
bool	V > &L	returns true if L is parallel to V and lies above V .
bool	V == &L	returns true if the lines are identical.

9.4 1-line-algorithms (lines)

1. Definition

An instance of the data type *lines* consists of 1-line algorithms.

2. Median-problems

double	$V.L_12_sum_M3(facilities\& features)$	acs)
		computes the optimum for problem class $LL/P/./l_2/\sum$ and returns the objective value.
double	V.L_l1_sum_M3(facilities& f	acs)
		computes the optimum for problem class $LL/P/./l_1/\sum$ and returns the objective value.
double	$V.L_linf_sum_M3(facilities\&$	facs)
		computes the optimum for problem class $lL/P/./l_{\infty}/\sum$ and returns the objective value.
double	V.L.lp_sum_M3(facilities& f	acs, int p)
		computes the optimum for problem class $LL/P/./l_p/\sum$ and returns the objective value.
double	$V.L_12_sum_M2\logM(facilities)$	$s\& \ facs)$
	С	computes the optimum for problem class

computes the optimum for problem class $1L/P/./l_2/\sum$ and returns the objective value.

double	$V.L_l2_sum_M2(facilities\&$	facs)
		computes the optimum for problem class $1L/P/v_i = 1/l_2/\sum$ and returns the objective value.
double	$V.{\tt L_block_sum_M3} (list < poly$	gauge > &LG, list < int > &Ln, facilities & facs)
		computes the optimum for problem class $1L/P/./l_{block}/\sum$ and returns the objective value.
3. Center-p	oroblems	
double	$V.L_12_max_M4(facilities\&$	facs)
		computes the optimum for problem class $1L/P/./l_2/max$ and returns the objective value.
double	$V.L_{l1}max_M4(facilities\&$	facs)
		computes the optimum for problem class $1L/P/./l_1/max$ and returns the objective value.
double	$V.L_linf_max_M4(facilities)$	& facs)
		computes the optimum for problem class $1L/P/./l_{\infty}/max$ and returns the objective value.
double	$V.\texttt{L_l2_max_MlogM}(faciliti$	es& facs)
		computes the optimum for problem class $1L/P/v_i = 1/l_2/max$ and returns the objective value.
double	$V.L_l2_max_M2logM(facilit$	ies& facs)
		computes the optimum for problem class $1L/P/./l_2/max$ and returns the objective value.
double	$V.L_lp_max_M4(facilities\&$	facs, int p)
		computes the optimum for problem class $1L/P/./l_p/max$ and returns the objective value.
double	V.L_block_max_M4(list <pol)< td=""><td>ygauge > &LG, list < int > &Ln, facilities & facs)</td></pol)<>	ygauge > &LG, list < int > &Ln, facilities & facs)
		computes the optimum for problem class $1L/P/./l_{block}/max$ and returns the objective value.

double	$V.lp_distance_2_line(location \& l$	1, location &12, location &L, int p)
		lculates the l_p -distance of L to the line defined $l1$ and $l2$.
double	$V.{ m objective_function_l2} (location$	$*locs, \ int \ start, \ int \ N, \ location \ \&l1, \ location \ \&l2)$
	wi an inc	lculates the value of the objective function th metric l_2 for the line defined by $l1$ and $l2$ d for the locations with <i>start</i> as the beginning dex (first element has to be 1) and N as the dex for the final element.
void	$V.$ max_line_l2(location &l1, local)	tion&l2, location&l3, location&r1, location&r2)
		lculates the optimal l_2 -line defined by $r1$ and for $l1$, $l2$ and $l3$.
double	$V.{ m objective_function_linf}(location)$	$pn*locs,\ intstart,\ intN,\ location\&result1,\ location\&result2)$
	wi an inc	lculates the value of the objective function th metric l_{∞} for the line defined by $l1$ and $l2$ d for the locations with <i>start</i> as the beginning dex (first element has to be 1) and N as the dex for the final element.
double	$V.{ m objective_function_l1} (location$	*locs, int start, int N, location & result 1, location & result 2)
	wi an inc	lculates the value of the objective function th metric l_1 for the line defined by $l1$ and $l2$ d for the locations with <i>start</i> as the beginning dex (first element has to be 1) and N as the dex for the final element.
void	$V.\max_line_1(location\&l1, local)$	tion&l2,location&l3,location&r1,location&r2)
		lculates the optimal l_1 -line defined by $r1$ and for $l1$, $l2$ and $l3$.
double	$V.{ m objective_function_lp}(location)$	$n*locs,\ intstart,\ intN,\ location\ \&result1,\ location\ \&result2,\ intpart N,\ ho\ \&result2,\ intpart N,\ ho\ \&result2,\ ho$
	wi an inc	lculates the value of the objective function th metric l_p for the line defined by $l1$ and $l2$ d for the locations with <i>start</i> as the beginning dex (first element has to be 1) and N as the dex for the final element.
void	$V.\max_line_lp(location \& l1, local)$	$tion \& l2, \ location \& l3, \ location \& r1, \ location \& r2, \ int \ p)$

4. Useful functions

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calculates the optimal l_p -line defined by r1 and r2 for l1, l2 and l3.

$V.{ m objective_function_block} (location * locs, int start, int N, location \& l1, location \& l2, Blocknorm location \& lacation & lacati$
calculates the value of the objective function with block-metric for the line defined by $l1$ and $l2$ and for the locations with <i>start</i> as the beginning index (first element has to be 1) and N as the index for the final element.
$V. \texttt{max_line_block} (location \& l1, location \& l2, location \& l3, location \& r1, location \& r2, Blocknorm and here a$
calculates the optimal <i>block</i> -line defined by $r1$ and $r2$ for $l1$, $l2$ and $l3$.
$V.geometric_duality(location * locs, location & pivot, int M)$
sorts all M locations <i>locs</i> with respect to <i>pivot</i> using geometric duality.
V.y-quicksort(location * tosort, int l, int r, location * old)
sorts the locations $tosort$ from l (usual 0) to r (usual number of locations minus 1) dependent on the y -coordinate (all locations have to be 2-dimensional) using a recursive quicksortalgorithm (old should be the last location).

5. Implementation

The time needed by the algorithms is given in the name of each, e.g. algorithm $L_{J2}_{max}M2 \log M$ takes $o(M^2 \log M)$ time to run.

9.5 Facilities (facilities)

1. Definition

An instance of the data type *facilities* consists of a list of locations.

2. Creation

facilities EX; introduces a variable EX of type facilities.

3. Operations

3.1 Input and Output

string	$EX.name(int \ location)$	provides a name for <i>location</i> .
void	$EX.set_name(int \ location, \ st$	tring &name)
		specifies a name for <i>location</i> .
void	EX.Write(ostream & out)	prints all facilities.
void	EX.WriteOpt(ostream & out)	prints the set of optimal solutions.

3.2 Operations

bool	EX.element $(location & Loc)$	returns true if Loc is an element of EX , else false.
location	$EX.get_element(int \ idx)$	returns the idx -element of the EX .
int	$EX.get_idx(location \&L)$	returns the index of L otherwise the total number of locations.
void	EX.remove(location &L)	removes L from EX if possible.
void	$EX.remove(int \ idx)$	removes the idx -element of EX if possible.
double	$EX.\max_direction_value(inti)$	returns the maximum value of coordinate i of all locations of EX .
double	$EX.min_direction_value(inti)$	returns the minimum value of coordinate i of all locations of EX .
double	$EX.diff_value(int i)$	returns the maximal difference between co- ordinates i of any two locations of EX .

3.3 Algorithms

3.3.1 Median-problems

double EX.11_sum(int weight, bool erase)

computes the optimum for problem class $1/P/./l_1/\sum$ and returns the objective value.

double	$EX.l2sqr_sum(int weight, bool \ erase)$	
		computes the optimum for problem class $1/P/./l_2^2/\sum$ and returns the objective value.
double	$EX.linf_sum(int weight, bool$	erase)
		computes the optimum for problem class $1/P/./l_{\infty}/\sum$ and returns the objective value.
double	$EX.l2_sum(int weight, double$	e epsilon, bool erase)
		computes the optimum for problem class $1/P/./l_2/\sum$ (Weiszfeld-Algorithm) and returns the objective value.
double	EX. Weiszfeld(double epsilon)	calls $l2_sum(0, epsilon, true)$.
double	$EX.{\rm lp_sum}(intp, doubleepsilon, doubledelta, intiter_max, intweight, boolerase)$	
		computes the optimum for problem class $1/P/./l_p/\sum$ (Generalized Weiszfeld- Algorithm) and returns the objective value.
double	$EX.l2sqr_qsum(bool\ erase)$	
		computes the optimum for problem class $1/P/./l_2^2/Q - \sum$ (Q-criterial problem) and returns the objective value.
double	$EX.l1_2sum(bool\ erase)$	
		computes the optimum for problem class $1/P/./l_1/2 - \sum$ (bi-criterial problem) and returns the objective value.
double	$EX.linf_2sum(bool\ erase)$	
		computes the optimum for problem class $1/P/./l_{\infty}/2 - \sum$ (bi-criterial problem) and returns the objective value.
double	$EX.N_l1_sum(int N, matrix\&$	$x w, bool \ erase)$
		computes the optimum for problem class $N/P/./l_1/\sum$ with matrix of interdependencies w and returns the objective value.
double	$EX.N_linf_sum(int N, matrix)$	$\& w, bool \ erase)$

computes the optimum for problem class $N/P/./l_{\infty}/\sum$ with matrix of interdependencies w and returns the objective value.

double	$EX.N_l2sqr_sum(int N, matr$	$EX.N_l2sqr_sum(int N, matrix\& w, bool \ erase)$	
		computes the optimum for problem class $N/P/./l_2^2/\sum$ with matrix of interdependencies w and returns the objective value.	
double	$EX.N_l2sqr_sum(int N, matr$	$ix\& w, bool \ erase)$	
		computes the optimum for problem class $N/P/./l_p/\sum$ (Version 1) and returns the objective value.	
double	$EX.N_l2sqr_sum(int N, matrix\& w, bool \ erase)$		
		computes the optimum for problem class $N/P/./l_p/\sum$ (Version 2) and returns the objective value.	
double	$EX.fn_sum(int n, int p)$	computes objective value of X_n regarding all locations of EX .	
double	$EX.fex_sum(int p)$	computes objective value of all solutions regarding all facilities.	
double	$EX.fnew_sum(matrix\& w, int p)$		
		computes objective value of X_n 's to each other.	
void	$EX.N_l1_sum_gen_LP(int N, matrix\& w, char * lp1, char * lp2)$		
		generates LP for problem class $N/P/./l_1/\sum$.	
void	$EX.write_mps(vector \& OBJ, filename)$	$matrix\&\ CONSTRAINTS, vector\&\ RHS, list < char>\&\ EQU, char>$	

		writes down a given objective func- tion vector OBJ , matrix of constraints CONSTRAINTS, right hand side vector RHS, (in)equality sign list EQU to file filename in mps-format. For each row of CONSTRAINTS there must be a corre- sponding entry in EQU of the set E(for equal to), L(for less than or equal to), G(for greater than or equal to), and N(for neutral). Remember that the objective row must not be mentioned in EQU . EQU is only for use with the $CONSTRAINT$ -rows.
double	$EX.gauge_sum(list < polygaug)$	e>& LG, list <int>& Ln, bool erase)</int>
		computes the optimum for problem class $1/P/./\gamma/\sum$.
double	EX.gauge_bi_crit_sum(list <po< td=""><td>lygauge>& LG, list<int>& Ln, bool erase)</int></td></po<>	lygauge>& LG, list <int>& Ln, bool erase)</int>
		computes the optimum for problem class $1/P/./\gamma/2 - \sum_{par}$ and returns the number of situations (line segments and cells) the pareto set consists of.
3.3.2 Center-	problems	
double	$EX.linf_max(bool\ erase = true)$	$\iota e)$
		computes the optimum for problem class $1/P/./l_{\infty}/max$ and returns the objective value.
double	$EX.l1_max(bool\ erase = true)$)
		computes the optimum for problem class $1/P/./l_1/max$ and returns the objective

value.

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double $EX.l1_v1_max(bool \ erase = true)$

computes the optimum for problem class $1/P/w_m = 1/l_1/max$ and returns the objective value.

double $EX.l2_max(bool \ erase = true)$

computes the optimum for problem class $1/P/./l_2/max$ and returns the objective value.

double	$EX.linf_v1_max(bool\ erase = true)$	
		computes the optimum for problem class $1/P/./l_{\infty}/max$ and returns the objective value.
double	$EX.elz_hearn(bool\ erase = tr$	(ue)
		computes the optimum for Elzinga-Hearn- Algorithm and returns the objective value.
double	$EX.N_linf_max(int N, matrix\& W, bool \ erase = true)$	
		computes the optimum for problem class $N/P/./l_{\infty}/max$ and returns the objective value.
double	$EX.N_{l1}_{max}(int N, matrix)$	$k W, bool \ erase = true)$
		computes the optimum for problem class $N/P/./l_1/max$ and returns the objective value.
double	$EX.N_linf_max_mps(int N, matrix\& W, bool \ erase = true)$	
		computes the optimum for problem class $N/P/./l_{\infty}/max$ using <i>mps</i> -files and CPLEX and returns the objective value. CPLEX generates also two files named "sol1.txt" and "sol2.txt".
double	$EX.N_{l1}_{max_mps}(int N, m$	$atrix\& W, bool \ erase = true)$
		computes the optimum for problem class $N/P/./l_1/max$ using <i>mps</i> -files and CPLEX and returns the objective value. CPLEX generates also two files named "sol1.txt" and "sol2.txt".
3.4 Useful Fu	inctions	
double	EX objective value computat	ion(list <polygauge>& La. list<int>& Ln. point X. ii</int></polygauge>

double	$EX.objective_value_computation(list\& Lg, list\& Ln, point X, int q)$
	computes the objective value for a gauge problem.
double	$EX.objective_value_computation(list\& Lg, list\& Ln, point X, int q)$
	computes the subgradient value for a gauge problem.

list <segment></segment>	$EX.all_segments_computation(list< polygauge>\& Lg, list< int>\& Ln, point Y, double f_X, int q)$
	computes all segments for all locations for 1-criterial.
list <segment></segment>	$EX. all_segments_computation(list< polygauge>\&\ Lg, list< int>\&\ Ln, point\ Y, double\ f_X, int\ q)$
	computes the function values for the grid- points.
vector	$EX. {\tt niveauline_vector_computation} (list < polygauge > \&\ Lg, list < int > \&\ Ln, point\ X, int\ q)$
	computes the direction vector for level curve.
list < point >	$EX.$ computation_of_lex_solutions($list < polygauge > \& Lg, list < int > \& Ln, point X, int q1, int q2, G$ computes the lexicographical solution.
list < location >	$EX. \texttt{non_trivial_case} (list < polygauge > \& Lg, list < int > \& Ln, list < point > \& Lex_sol_12, lis$
	computes the pareto solution for a non trivial case.

9.6 Facilities-utilities (facs_util)

1. Definition

An instance EX of the data type facs_util supports the data type facilities. It provides some useful routines to handle the class facilities.

2. Creation

 $facs_util EX$; creates a list of location EX of type $facs_util$.

3. Operations

3.1 Input and Output

void = EX.ReadLoc(ifstream&file) reads all locations from file.

 $void = EX.ReadLoc_Res(if stream \& file) ds all locations with results from file.$

void EX.ReadLoc(ifstream& file, list<int>& Dist)

reads all locations from file and returns a list to associate distance functions.

- void = EX.ReadRestr(ifstream& file) reads all restrictions from file.
- void = EX.SaveLoc(ostream& file) saves all locations into file.
- *void* EX.SaveLoc_Res(*ostream*& *file*, *double objval*, *string normact*)

saves all locations and the results of the current problem into file.

- $matrix \quad EX. {
 m ReadMat}(ifstream\&\,file) \ {
 m reads a matrix from }file \ {
 m for a } multi-facilities-problem.$
- *void* EX.View(double objval, string normact, list<location>& AlgSol, restrictions& Restr)

shows the results and locations of the current problem.

void = EX. View (double objval, string normact, list < location > & AlgSol, restrictions & Restr, list < polygauge > and the string normal s

shows the results and locations of the current problem.

 $void \qquad EX. \\ View (double \ objval, string \ normact, list < location > \& \ AlgSol, restrictions \& \ Restr, \ list < polygon > \& \ AlgSol, restrictions \& \ Restr, \ list < polygon > \& \ Restr, \ Restr, \ list < polygon > \& \ Restr, \ R$

shows the results and locations of the current problem.

 $void \qquad EX. \ensuremath{\mathsf{View}}(double\ objval,\ string\ normact,\ list < location > \&\ AlgSol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restr,\ list < polygon > \&\ Sol,\ restrictions \&\ Restrictions &\ Restrictions \ Restrictions \ Restrictions \ Restrictions \ Restrictions \ Restr,\ restrictions \ Restrictions \ Re$

shows the results and locations of the current problem.

Restricted Planar Classes

10.1 Restriction (restriction)

1. Definition

Restriction is one of three restriction-types (*restr_poly*, *restr_circle* or *restr_rect*) and has the following virtual function for all of them.

2. Creation

restriction R; creates a variable R of type restriction.

3. Operations

int	$\operatorname{type}()$	returns the type of the restriction $(restr_p, restr_c \text{ or } restr_r).$
bool	$\mathrm{inout}()$	returns true if the forbidden region should be inside R , false otherwise.
void	in_forbid()	changes forbidden region to inside.
void	$out_forbid()$	changes forbidden region to outside.
bool	inside(point p)	returns true if p lies inside R , false otherwise.
bool	inside(location Loc)	returns true if Loc lies inside R , false otherwise.
bool	inside(segment seg)	returns true if seg lies inside R , false otherwise.

$\mathit{list}<\!\mathit{point}>$	intersect(ray r)	returns $R \cap r$ as a list of points.
list < point >	intersection(line l)	returns $R \cap l$ as a list of points.
list < point >	intersection(segment s)	returns $R \cap s$ as a list of points.
list < point >	intersection(polygon P)	returns $R \cap P$ as a list of points.
list < point >	intersection(circle C)	returns $R \cap C$ as a list of points.
list < location >	$proj_l2sqr(location opt)$	returns the projected locations for the l_2^2 Norm.
double	proj_v1_l2_max(location op	pt, facilities facs, double z_opt)
		returns the objective value for the projected solution in opt for the

projected solution in opt for the problem class $1/P/w_m = 1/l_2/max$.

Non-virtual functions

bool	$inside_all(restriction* restrict, list < location > opt)$	
	returns true if all locations lie inside the restriction, false otherwise.	
restriction*	$inside_which(list < restriction * > restrict, location loc)$	
	returns <i>restriction</i> where <i>loc</i> lies inside.	
restriction*	$inside_which(list < restriction * > restrict, segment seg);$	
	returns $restriction$ where seg lies inside.	
restriction*	$inside_which(list restrict, list opt);$	
	returns $restriction$ where all locations from opt lie inside.	

10.2 Polygon as a restriction (restr_poly)

1. Definition

An instance P of the data type $restr_poly$ is a simple polygon in the two-dimensional plane defined by the sequence of its vertices. The number of vertices is called the size of P. A $restr_poly$ with empty vertex sequence is called empty.

2. Creation

 $restr_poly P;$

introduces a variable P of type $restr_poly$. P is initialized to the empty $restr_poly$.

 $restr_poly P(list < point > p);$

introduces a variable P of type restr_poly. P is initialized to the restr_poly with vertex sequence p. *Precondition*: The vertices in p define a simple polygon.

3. Operations

list <point></point>	P.vertices()
0000 1 000000	1.1010000()

returns the sequence of vertices of P in counterclockwise ordering.

list < segment >	P.segments()	returns the sequence of bounding segments of P in counterclockwise ordering.
bool	$P. ext{convex}()$	returns true if P is convex, false otherwise.
int	P.size()	returns the size of P .
bool	$P. ext{empty}()$	returns true if P is empty, false otherwise.
bool	$P.==(restr_poly P1)$	test for equality of P and $P1$.

10.3 Circle as a restriction (restr_circle)

1. Definition

An instance C of the data type *restr_circle* is a circle in the two-dimensional plane, i.e. the set of points having a certain distance r from a given point p. r is called the radius and p is called the center of C. The *restr_circle* with center (0,0) and radius 0 is called the empty *restr_circle*.

2. Creation

 $restr_circle$ C;

introduces a variable C of type $restr_circle$. C is initialized to the empty $restr_circle$.

 $restr_circle \quad C(point \ c, \ double \ r);$

introduces a variable C of type *restr_circle*. C is initialized to the circle with center c and radius r.

restr_circle C(double x, double y, double r);

introduces a variable C of type restr_circle. C is initialized to the circle with center (x, y) and radius r.

restr_circle C(point a, point b, point c);

introduces a variable C of type restr_circle. C is initialized to the circle through points a, b, and c. Precondition: a, b, and c are not collinear.

3. Operations

point	C.center()	returns the center of C .
double	C.radius()	returns the radius of C .
double	$C.distance(point \ p)$	returns the distance between C and p (negative if p inside C).
bool	C == D	tests for equality of C and D .

10.4 Rectangle as a restriction (restr_rect)

1. Definition

An instance R of the data type $restr_rect$ is a simple rectangle in the two-dimensional plane defined by the sequence of its vertices. The number of vertices is called the size of R. A restr_rect with empty vertex sequence is called empty.

2. Creation

restr_rect R(point p, double x, double y, double rad);

introduces a variable R of type restr_rect. R is initialized to the restr_rect with corner p and sides of length x and y and rotated by rad.

restr_rect R(point p, double x, double y);

introduces a variable R of type *restr_rect*. R is initialized to the *restr_rect* with corner p and sides of length x and y.

restr_rect $R(point \ p1, point \ p2, point \ p3, point \ p4);$

introduces a variable R of type restr_rect. R is initialized to the restr_rect with vertices p1, p2, p3, p4.

 $restr_rect \ R(point \ p1, point \ p2);$

introduces a variable R of type *restr_rect*. R is initialized to the *restr_rect* with opposite vertices p1 and p2.

3. Operations

double	R.area()	returns the area of R .
int	$R.==(restr_rect \ r1)$	tests for equality of R and $r1$.

10.5 Algorithms for Forbidden Regions (restrictions)

1. Definition

An instance of the data type *restrictions* consists of the algorithm to solve planar location problems with restrictions.

2. Creation

restrictions R; creates restrictions R

3. Operations

list<location> R.alg_solution() returns the solution for the current problem.

double $R.ll_sum(facilities\& EX, bool erase)$

computes the optimum for problem class $1/P/R/l_1/\sum$ and returns the objective value.

double R.linf_sum(facilities & EX, bool erase)

computes the optimum for problem class $1/P/R/l_{\infty}/\sum$ and returns the objective value.

double $R.12sqr_sum(facilities\& EX, bool \ erase)$

computes the optimum for problem class $1/P/R/l_2^2/\sum$ and returns the objective value.

double R.lp_sum(facilities& EX, int p, double epsilon, double delta, int iter_max, bool erase)

computes the optimum for problem class $1/P/R/l_p/\sum$ and returns the objective value.

double $R.l2_v1_max(facilities\& EX, bool \ erase)$

		computes the optimum for problem class $1/P/R = convex polyhedron, w_m = 1/l_1/\sum$ and returns the objective value.
double	$R.linf_max(facilities\& EX,$	bool erase)
		computes the optimum for problem class $1/P/R = convex restriction/l_{\infty} / \sum$ and returns the objective value.
double	$R.l1_max(facilities \& EX, bool \ erase)$	
		computes the optimum for problem class $1/P/R = convex restriction/l_1 / \sum$ and returns the objective value.
double	$R.L_RkonvPoly_l2_sum(faci)$	lities & EX, bool erase)
		computes the optimum for problem class $1L/P/R = convex polyhedron/l_2/\sum$ and returns the objective value.
double	$R.L_RkonvPoly_lp_sum(faci$	lities & EX, bool erase, int norm)
		computes the optimum for problem class $1L/P/R = convex polyhedron/l_p/\sum$ and returns the objective value.
double	$R.L_RkonvPoly_lp_sum(fact)$	lities& EX, bool erase, int norm)
		computes the optimum for problem class $1L/P/R = convex polyhedron/l_1/\sum$ and returns the objective value.
double	$R.L_RkonvPoly_lp_sum(faci$	lities & EX, bool erase, int norm)
		computes the optimum for problem class $1L/P/R = convex polyhedron/l_{\infty}/\sum$ and returns the objective value.
double	$R.L_RkonvPoly_lp_sum(fact)$	lities & EX, bool erase, int norm)
		computes the optimum for problem class $1L/P/R = convex \ polyhedron/\gamma_B/\sum$ and returns the objective value.

10.6 Polygon as a barrier (polygon_barrier)

1. Definition

An instance P of the data type *polygon_barrier* is a simple polygon in the two-dimensional plane defined by the sequence of its vertices. The number of vertices is called the size of P. A *polygon_barrier* with empty vertex sequence is called empty.

2. Creation

polygon.	barrier	P
porggon.		- 1 :

introduces a variable P of type $polygon_barrier$. P is initialized to the empty $polygon_barrier$.

 $polygon_barrier P(list < point > Pt);$

introduces a variable P of type polygon_barrier. P is initialized to the polygon with vertex sequence Pt. Precondition: The vertices in Pt define a simple polygon.

3. Operations

list <point></point>	P.vertices()	returns the sequence of vertices of P in counterclockwise ordering.
bool	P.visible(point & p1, point & p2) turns true if $p2$ is visible from $p1$ with respector to $P.$	

10.7 Circle as a barrier (circle_barrier)

1. Definition

An instance C of the data type *circle_barrier* is a circle in the two-dimensional plane, i.e. the set of points having a certain distance r from a given point p. r is called the radius and p is called the center of C. The *circle_barrier* with center (0,0) and radius 0 is called the empty *circle_barrier*.

2. Creation

circle_barrier C;

introduces a variable C of type *circle_barrier*. C is initialized to the empty *circle_barrier*.

circle_barrier $C(point \ p, double \ r);$

introduces a variable C of type *circle_barrier*. C is initialized to the circle with center p and radius r.

circle_barrier C(double x, double y, double r);

introduces a variable C of type circle_barrier. C is initialized to the circle with center (x, y) and radius r.

circle_barrier C(point a, point b, point c);

introduces a variable C of type *circle_barrier*. C is initialized to the circle through points a, b, and c. *Precondition*: a, b, and c are not collinear.

3. Operations

point	C.center()	returns the center of C .
double	C.radius()	returns the radius of C .
bool	C.visible(point p1, point p2)	returns true if $p2$ is visible from $p1$ with respect to P .

10.8 Segment as a barrier (segment_barrier)

1. Definition

An instance S of the data type *segment_barrier* is a segment in the two-dimensional plane defined by its the points including the segment.

2. Creation

 $segment_barrier S;$

introduces a variable S of type $segment_barrier$. S is initialized to the empty $segment_barrier$.

 $segment_barrier S(point p1, point p2);$

introduces a variable S of type segment_barrier. S is initialized to the segment (p1, p2).

3. Operations

point	$S.\mathrm{point1}()$	returns the source point of S .
point	$S.\mathrm{point2}()$	returns the target point of S .
bool	S.visible(point, point)	returns true if $p2$ is visible from $p1$ with respect to P .

10.9 Algorithms for Barriers (barrier)

double $S.12_sum(facilities\& EX, bool erase, int choose = 1, double percent = 0.1, double accel = 1.0, double init_ss = 0.01, double epsilon = 0.001)$

computes the optimum for problem class $1/P/(R,\infty)/l_2/\sum$ and returns the objective value.

10.10 Restriction-utilities (restr_util)

Restriction-utilities provides useful routines to handle restrictions.

double	Restr_max_dir(int i, restrictions Restr)	
		returns the maximal coordinate in direction i ($i = 0$ x-coordinate, $i = 1$ y-coordinate).
double	Restr_min_dir(int i, restrie	ctions Restr)
		returns the minimal coordinate in direction i ($i = 0$ x-coordinate, $i = 1$ y-coordinate).
double	Restr_diff_value(int i, rest	rictions Restr)
		returns the maximal difference between the coordinates in direction i (i = 0 x-coordinate, $i = 1 y$ -coordinate).
void	DrawRestr(window W, re	strictions Restr)
		draws the restrictions in a window W .
restrictions	ReadRestr(ifstream file)	
		returns the restrictions given in the correct format in <i>file</i> .

$restr_poly$	$\operatorname{ReadPoly}(\operatorname{ifstream}\operatorname{file})$	
		returns a polygon as a restriction given in the correct format in <i>file</i> .
$restr_circle$	$\operatorname{ReadCirc}(\operatorname{ifstream} \operatorname{file})$	
		returns a circle as a restriction given in the correct format in $file$.
restr_rect	ReadRect(ifstream file)	returns a rectangle as a restriction given in the correct format in <i>file</i> .

Planar Classes with Gauges

11.1 Polyhedral Gauges (polygauge)

1. Definition

An instance G of the data type *polygauge* is a gauge in the two-dimensional plane defined by the sequence of its vertices in counterclockwise order which creates the cones. These cones are numbered in counterclockwise order. The number of vertices is called the size of G. See also the Gauge-utilities header (gauge_util.h), which provides Load, Save, Create and View for Gauges.

2. Creation

 $polygauge \quad G(list < point > pl);$

introduces a variable G of type *polygauge*. G is initialized to the polygauge with vertex sequence pl.

Precondition: The vertices in pl are given in counterclockwise order and define a polygauge. The polyhedral belonging to the polygauge must be convex.

polygauge G;

introduces a variable G of type *polygauge*. G is initialized to the empty polygauge.

3. Operations

point	$G \ [int \ c]$	returns the c -th extreme point of G .
point	G.origin()	returns the origin G .

list < point >	G.vertices()	returns the vertex sequence of G for the reference point $origin$.
list < point >	$G.vertices(point \ r)$	returns the vertex sequence of G for the reference point r .
list < point >	$G.vertices(location \ rl)$	returns the vertex sequence of G for the reference location rl .
list < segment >	G.segments(point r)	returns the sequence of bounding segments of the cones of G in counterclockwise order for the reference point r .
list < segment >	$G.segments(location \ rl)$	returns the sequence of bounding segments of the cones of G in counterclockwise order for the reference location rl .
list < double >	G.alphas()	returns the angle sequence of G
list <point></point>	$G. ext{conepoints}(pointr,intc)$	returns the extreme points creating the cone c .
list < point >	$G.$ conepoints $(location \ rl, \ a)$	int c)
		returns the extreme points creating the cone c .
list < segment >	$G.coneseg(point \ r, \ int \ c)$	returns the segments creating the cone c .
list < segment >	$G.coneseg(location \ rl, \ int$	<i>c</i>)
		returns the segments creating the cone c .
int	G.conetest(point r, int c,	$point \ p, \ bool \& \ unique)$
		returns 1 if p lies inside the cone c , 0 otherwise; if p lies on a segment border, unique is false; if r is equal to p , 0 is returned and unique is false.
int	$G.conetest(location \ rl, \ int$	c, location l, bool& unique)
		returns 1 if l lies inside the cone c , 0 otherwise; if l lies on a segment border, unique is false; if rl is equal to l , 0 is returned and unique is false.
int	G.inCone(point r, point p,	, bool& unique)
		returns the number of the cone, p lies inside; if p lies on a segment border, unique is false; if r is equal p , 0 is returned and unique is false.

int	$G.inCone(location \ rl, \ location \ l, \ bool\& \ unique)$	
		returns the number of the cone, l lies inside; if l lies on a segment border, unique is false; if rl is equal to l , 0 is returned and unique is false.
list < point >	$G.pl_inCone(point r, int c$, list <point> pl)</point>
		returns the list of points pl which lie inside the cone c , returns the empty list if no point is inside the cone.
list < location >	$G.ll_inCone(location \ rl, \ ir)$	nt c, list <location> ll)</location>
		returns the list of locations of ll which lie inside the cone c , returns the empty list if no location is inside the cone.
double	G.norm(point r, point p)	returns the norm for the gauge from point r to point p .
double	$G.norm(location \ rl, \ locati$	on l)
		returns the norm for the gauge from location rl to location l .
list <double></double>	$G.lin_describe(point r, int c$	(i) returns m (in list.head()) and b (in list.tail()) as the linear description $(y = m \cdot x + b)$ of the cone c ; returns inf (in list.head()) and x (in list.tail()) if segment is vertical.
list <double></double>	$G.lin_describe(location \ rl,$	int c)
		returns m (in list.head()) and b (in list.tail()) as the linear description $(y = m \cdot x + b)$ of the cone c , returns inf (in list.head()) and x (in list.tail()) if segment is vertical.
double	$G.\max_dist()$	returns the maximal euclidean distance from origin of the gauge G to the extreme points.
point	$G.\max(point \ r, int \ i)$	returns the extreme point of G with the maximal coordinate, $i=0$ for x-coord and $i=1$ for y-coord.
point	$G.mini(point \ r, int \ i)$	returns the extreme point of G with the minimal coordinate, $i=0$ for x-coord and $i=1$ for y-coord.
point	$G.$ maxi $(location \ rl, int \ i)$	returns the extreme point of G with the maximal coordinate, $i=0$ for x-coord and $i=1$ for y-coord.

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point	G.mini(location rl, int i)	returns the extreme point of G with the minimal coordinate, $i=0$ for x-coord and $i=1$ for y-coord.
double	$G.\max_diff(int \ i)$	returns the difference between $max i$ and min , i=0 for x-coord and $i=1$ for y-coord.
polygauge	$G.{ m dual}()$	returns the dual gauge of G .
polygauge	$G.rotate(double \ alpha)$	returns the gauge created by a rotation of G by angle $alpha$.
polygauge	G.l1()	returns the l_1 gauge.
polygauge	$G.\mathrm{linf}()$	returns the l_{∞} gauge.
polygauge	$G.\mathrm{unit}()$	returns the gauge with all segments of length 1.
polygauge	$G.join(polygauge\&\ H)$	returns the union of gauge G and H .
polygauge	$G.scale(double \ scale)$	returns the gauge with all segments scaled with $scale$.
polygauge	$G.translate(point \ r)$	returns the gauge with all segments translated to r .
bool	G. symmetrical()	returns true if G is symmetrical, false otherwise.
int	G.size()	returns the size of G .
bool	$G.\mathrm{empty}()$	returns true if G is empty, false otherwise.
bool	G == H	tests for equality of G and H .
bool	G != H	tests for inequality of G and H .

11.2 Mixed Gauges (mixgauge)

1. Definition

An instance G of the data type *mixgauge* is a gauge in the two-dimensional plane defined by the sequence of its vertices in counterclockwise order which creates the cones. These cones are numbered in counterclockwise order. The number of vertices is called the size of G. See also the Gauge-utilities header (gauge_util.h), which provides Load, Save, Create and View for Gauges.

11.2. MIXED GAUGES (MIXGAUGE)

2. Creation

mixgauge G(list<point> pl, list<bool> typ);

introduces a variable G of type mixgauge. G is initialized to the mixgauge with vertex sequence pl. *Precondition*: The vertices in pl are given in counterclockwise order and define a mixgauge. The polyhedral belonging to the mixgauge must be convex.

mixgauge G;

introduces a variable G of type mixgauge. G is initialized to the empty mixgauge.

3. Operations

point	G [int c]	returns the c -th extreme point of G .
bool	G.conetype(int c)	returns the type of the cone c .
list < point >	$G.vertices(point \ r)$	returns the vertex sequence of G for the reference point r .
list < point >	$G.vertices(location \ rl)$	returns the vertex sequence of G for the reference location rl .
list < segment >	$G.segments(point \ r)$	returns the sequence of bounding segments of the cones of G in counterclockwise order.
list < segment >	$G.segments(location \ rl)$	returns the sequence of bounding segments of the cones of G in counterclockwise order.
list < double >	$G.\mathrm{alphas}()$	returns the angle sequence of G .
list <point></point>	G.conepoints $(point r, int c)$	returns the extreme points creating the cone c .
list <point></point>	$G.$ conepoints $(location \ rl, \ a)$	int c)
		returns the extreme points creating the cone c .
list <segment></segment>	G.coneseg(point r, int c)	returns the segments creating the cone c .
list <segment></segment>	$G.coneseg(location \ rl, \ int$	c)

returns the segments creating the cone c.

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int	G.conetest(point r, int c,	$point \ p, \ bool \& \ unique)$
		returns 1 if p lies inside the cone c , 0 otherwise; if p lies on a segment border, unique is false; if r is equal to p , 0 is returned and unique is false.
int	$G.conetest(location \ rl, \ integral of the second secon$	$t \ c, \ location \ l, \ bool \& \ unique)$
		returns 1 if l lies inside the cone c , 0 otherwise; if l lies on a segment border, unique is false; if rl is equal to l , 0 is returned and unique is false.
int	G.inCone(point r, point p)	, bool $unique$)
		returns the number of the cone, p lies inside; if p lies on a segment border, unique is false; if r is equal to p , 0 is returned and unique is false.
int	G.inCone(location rl , loca	tion l, bool& $unique$)
		returns the number of the cone, l lies inside; if l lies on a segment border, unique is false; if rl is equal to l , 0 is returned and unique is false.
list <point></point>	G.pl_inCone(point r, int c, list <point> pl)</point>	
		returns the list of points which lie inside the cone c , returns the empty list if no point is inside the cone.
list < location >	$G.ll_inCone(location \ rl, \ ir$	nt c, list <location> ll)</location>
		returns the list of locations which lie inside the cone c , returns the empty list if no location is inside the cone.
double	G.norm(point r, point p)	returns the norm for the gauge from point r to point p .
double	$G.norm(location \ rl, \ locati$	on l)
		returns the norm for the gauge from location rl to location l .
list < double >	$G.lin_describe(point r, int$	c)
		returns m (in list.head()) and b (in list.tail()) as the linear description $(y = m \cdot x + b)$ of the cone c ; returns inf (in list.head()) and x (in list.tail()) if segment is vertical.

iisi\uouoie>	G.Im_describe(<i>iocation ri</i> ,	
		returns m (in list.head()) and b (in list.tail()) as the linear description $(y = m \cdot x + b)$ of the cone c , returns inf (in list.head()) and x (in list.tail()) if segment is vertical.
point	$G.maxi(point \ r, int \ i)$	returns the extreme point with the maximal coordinate, $i=0$ for x-coord and $i=1$ for y-coord.
point	$G.mini(point \ r, int \ i)$	returns the extreme point with the minimal coordinate, $i=0$ for x-coord and $i=1$ for y-coord.
point	$G.maxi(location \ rl, int \ i)$	returns the extreme point with the maximal coordinate, $i=0$ for x-coord and $i=1$ for y-coord.
point	$G.mini(location \ rl, int \ i)$	returns the extreme point with the minimal coordinate, $i=0$ for x-coord and $i=1$ for y-coord.
double	$G.\max_diff(int \ i)$	returns the difference between $max i$ and $min i$, i=0 for x-coord and $i=1$ for y-coord.
mixgauge	$G.{ m dual}()$	returns the dual gauge of G .
mixgauge	$G.rotate(double \ alpha)$	returns the gauge created by a rotation of G by angle $alpha$.
mixgauge	G.join(mixgauge& H)	returns the union of gauge G and H .
mixgauge	$G.\mathrm{unit}()$	returns the gauge with all segments of length 1.
mixgauge	$G.scale(double \ scale)$	returns the gauge with all segments scaled with $scale$.
bool	G. symmetrical()	returns true if G is symmetrical, false otherwise.
int	$G.{ m size}()$	returns the size of G .
bool	$G.\mathrm{empty}()$	returns true if G is empty, false otherwise.
bool	G == H	tests for equality of G and H .
bool	G != H	tests for inequality of G and H .

11.3 Gauge-utilities (gauge_util)

Gauge-utilities provides useful routines to handle gauges.

list<polygauge> ReadLPGauge(ifstream file) returns the list of polygauges. *list<mixqauqe>* ReadLMGauge(ifstream file) returns the list of mixgauges. list<int> ReadGNumber(ifstream file) returns the list of numbers to connect the locations with their gauges. Precondition: size of facilities is equal to size of numbers. voidSaveGauge(ofstream file, polygauge G) saves the list of extremal points from polygauge G in file. SaveGauge(ofstream file, mixgauge M) void saves the list of extremal points and the conetyp from mixgauge M in file. voidDrawGauge(window W, polygauge G) draws a polygauge G in a window W. voidDrawGauge(window W, mixgauge M) draws a mixgauge M in a window W. voidViewGauge(polygauge G) opens a window and a panel where you can choose Load, Save or Create a polygauge. voidViewGauge(mixgauge M) opens a window and a panel where you can choose Load, Save or Create a mixgauge.

Input-format for the files

ReadGauge(file)	begin {polygauge} $x_1 y_1$:
ReadGauge(file,tl)	$egin{array}{ccc} x_n & y_n \ ext{end} & \{ ext{polygauge}\} \ ext{begin} & \{ ext{mixgauge}\} \ x_1 & y_1 & typ_1 \end{array}$
ReadLPGauge(file)	: $x_n y_n typ_n$ end {mixgauge} begin {polygaugelist} begin {polygauge} $x_1 y_1$
ReadLMGauge(file)	$ \begin{array}{l} \vdots \\ x_n y_n \\ \text{end } \{ \text{polygauge} \} \\ \vdots \\ \text{begin } \{ \text{polygauge} \} \\ x_1 y_1 \\ \vdots \\ x_m y_m \\ \text{end } \{ \text{polygauge} \} \\ \text{begin } \{ \text{mixgauge} \} \\ \text{begin } \{ \text{mixgauge} \} \\ x_1 y_1 typ_1 \\ \vdots \\ x_n y_n typ_n \\ \text{end } \{ \text{mixgauge} \} \\ . \end{array} $
ReadGNumber(file)	: begin {mixgauge} $x_1 y_1 typ_1$: $x_m y_m typ_m$ end {mixgauge} end {mixgaugelist} begin {gaugenumber} num_1 : num_n end {gaugenumber}

Graph Classes

12.1 Basic Classes for Graphs (sol_typ, edge_segment, node_weight in graphsolution.h)

1. Definition

An instance of the data type sol_typ consists of two integers and one double to describe the solution of non restrictive problems. sol_typ is used to denote a location along the edge, where the integers describe the adjacent nodes and the double is a parameter $t \in [0..1]$ to give the position along the edge.

$sol_typ S;$	creates an instance of <i>sol_typ</i> .
S.source:=i;	defines the startnode i of edge e .
S.target:=j;	defines the endnode j of edge e .
S.alpha_s:=t;	defines the point t on edge e .

2. Definition

An instance of the data type *edge_segment* is derived from the data type *sol_typ* with an additional double to describe the solution of restrictive problems. *edge_segment* is used to denote a part of an edge.

edge_segment ES; creates an instance of edge_segment.

ES.source:=i;	defines the start node i of edge e .
ES.target:=j;	defines the endnode j of edge e .

 $\text{ES.alpha_s:=} t_1; \quad \text{defines the starting point } t_1 \text{ on edge } e. \\$

ES.alpha_t:= t_2 ; defines the endpoint t_2 on edge e.

3. Definition

An instance of the data type $node_weight$ is a list of doubles. A lolagraph uses this data-type as node-type.

12.2 Lolagraph (classlolagraph)

1. Definition

An instance of the data type *lolagraph* consists of a LEDA-Graph graph<node_weight, double>.

2. Creation

lolagraph G; creates a LEDA-Graph graph<node_weight, double> G

3. Operations

3.1 Helpfunctions

matrix	$G.\mathrm{shortest_path}()$	returns the distance matrix for the graph G .
edge		returns the edge between node v and node w in graph G .

3.2 Algorithms

list <sol_typ></sol_typ>	$G.abs_cent(double\& objval)$	returns the solution of the 1-center prob- lem of a whole graph, directed and undi- rected.
list <sol_typ></sol_typ>	G.center(double&)	returns the solution of the 1-center prob- lem on the nodes of a graph.
$list < sol_typ >$	G.median(char wert, double&	objval)
		returns the solution of the 1-median problem of the nodes for a directed or undirected graph.

$list < sol_typ >$	$G.N_median(int , double\&, list < int>\& belong to)$	
		returns the solution of the N-median problem of the nodes for a directed or undirected graph.
$list < sol_typ >$	$G. N_partitioning(int N, double)$	e& objval, list <int>& belongto, bool typ)</int>
		returns the solution of the N- median($typ=1$) or N-Center($typ=0$) problem of the nodes for a directed or undirected graph, using the "node- partitioning-heuristic".
list <sol_typ></sol_typ>	$G.{ m Nmed_exchange}(int~N,dou$	<pre>ble& objval, list<int>& belongto)</int></pre>
		returns the solution of the N-median problem of the nodes for a directed or undirected graph, using the "exchange- heuristic" .
$list < sol_typ >$	$G.N_greedy(int N, double\& o$	bjval,list <int>& belongto,bool typ)</int>
		returns the solution of the N-median $(typ=1)$ or N-center $(typ=0)$ problem of the nodes for an undirected graph, using the "greedy-heuristic".

12.3 Directed Graphs (loladirected)

1. Definition

An instance of the data type *loladirected* is a directed graph derived of the data type *lolagraph*.

2. Creation

loladirected GD; creates a directed lolagraph GD.

3. Operations

 $\label{eq:gd_sol_typ} GD. {\rm inmedian}(double \& \, objval) \mbox{ returns the solution of the 1-inmedian} \\ {\rm problem \, of \, the \, nodes \, for \, a \, directed \, graph}.$

list<sol_typ> GD.outmedian(*double*& objval)

returns the solution of the 1-outmedian problem of the nodes for a directed graph.

12.4 Undirected Graphs (lolaundirected)

1. Definition

An instance of the data type *lolaundirected* is a undirected graph derived of the data type *lolagraph*.

2. Creation

lola undirected GU; creates a undirected lolagraph GU.

3. Operations

 $list < sol_typ > \qquad GU.abs_med(double \& objval) \quad returns \ the \ solution \ of \ the \ 1-median \\ problem \ of \ a \ whole \ graph.$

12.5 Trees (lolatree)

1. Definition

An instance of the data type *lolatree* is a special undirected *lolagraph*, containing no loops. It is derived from the data type *lolaundirected*.

2. Creation

lolatree T; creates a lolatree T.

3. Operations

3.1 Helpfunctions

bool

 $T.is_tree()$

tests if G is a tree, i.e. containing no loops.

3.2 Algorithms

list<sol_typ> T.tree_node_med(*double*& objval)

		returns the solution of the local 1-median problem on a tree.
list <sol_typ></sol_typ>	$T.tree_med(double\& ob)$	jval)
		returns the solution of the absolute 1-median problem on a tree.
$list < sol_typ >$	$T.tree_center(double\& d$	objval)
		returns the solution of the absolute 1-center problem on a tree.
list <sol_typ></sol_typ>	$T.two_tree_center(doubl$	$e\& \ objval)$
		returns the solution of the absolute 2-center problem on a tree.
list <sol_typ></sol_typ>	$T.tree_node_center(double)$	ble& objval)
		returns the solution of the local 1-center prob- lem on a tree.

12.6 Graph-utilities (graph_util)

1. Definition

An instance of the data type graph_util supports the data type lolagraph. It is derived from the data type lolagraph. The class graph_util provides input and output routines to handle the class lolagraph.

2. Creation

 $graph_util G$; creates a lolagraph as graph_util G.

3. Operations

Input and Output

void	$G.QGraphView(list < vector > objvec, string normact, facilities \& EX, list < string > \& Loctxt, list < edge_segment > \& EL, bool dir)$	
	draws a lolagraph.	
lolagraph	$G.CreateGraph(string \ locfile, \ string \ adjfile, \ facilities\& \ EX)$	

96	CHAPTER 12. GRAPH CLASSES
	creates a lolagraph file and returns a parameterized graph and the facilities EX .
void	$G. {\tt SaveGraph} (of stream \& file, facilities \& EX, list {\tt string} {\tt \& Loctxt})$
	saves a lolagraph in a file.
void	G.SaveAdjlist(of stream & file)
	saves the adjacent list of a lolagraph in a file.
$graph_util\&$	$G. {\tt ReadGraph}(ifstream \&\ file,\ facilities \&\ EX,\ list {\tt string} {\tt \&\ Loctxt})$
	reads a lolagraph file and returns a param- eterized graph and the facilities EX .

Discrete Classes

13.1 Discrete Locations (discrete)

1. Definition

An instance of the data type *discrete* two list of location giving the positions for the demand and the supply points, and a matrix with travelling costs from a supply point to a demand point.

2. Creation

discrete D(matrix Cost);

introduces a variable D of type *discrete*. D is initialized with the cost matrix M.

3. Operations

3.1 Input and Output

void	D.ReadDiscrete($ifstream&file$)ads all data for D from $file$.		
void	$D.{ m DiscView}(double\ objval)$		
		shows the results and locations of the current problem.	
void	$D. {\it SaveDisc}(of stream \&\ file)$	saves all data of D into $file$.	

3.2 Algorithms

98		CHAPTER 13. DISCRETE CLASSES
double	$D.\mathrm{UFLP_greedy}()$	
		returns the solution of the UFL problem using the "greedy-heuristic" .
double	$D.\mathrm{UFLP_stingy}()$	
		returns the solution of the UFL problem using the "stingy-heuristic" .
double	$D.{ m UFLP_Interchange}()$	
		returns the solution of the UFL problem using the "interchange-heuristic" .
double	$D.\mathrm{UFLP_dualoc}()$	
		returns the solution of the UFL problem using the dualoc as an exact algorithm .

User Interface Class to LOLA

14.1 Algorithm (planealg)

1. Definition

An instance of the data type *planealg* consists of the algorithm to solve planar location problems.

2. Creation

planealg P; creates a variable P of type planealg.

3. Operations

list<location> P.alg_solution() returns the solution for the current problem.

void P.WriteOpt(ostream& out) writes the solution for the current problem.

3.1 Algorithms

3.1.1 Median-problems

double	$P.l1_sum(facilities\& EX)$	$\operatorname{computes}$	the	optimum	for	$\operatorname{problem}$	$_{\rm class}$
		$1/P/./l_1/2$	\sum an	d returns	the o	bjective v	alue.

double $P.ll_sum(facilities\& EX, restrictions\& R)$

computes the optimum for problem class $1/P/R = convex/l_1 / \sum$ (Konstukrionslinienalgorithmus) and returns the objective value.

100	CHAPTER 14. USER INTERFACE CLASS TO LOLA
double	$P.l2sqr_sum(facilities\&\ EX)$
	computes the optimum for problem class $1/P/./l_2^2/\sum$ and returns the objective value.
double	$P.12$ sqr_sum(facilities & EX, restrictions & R)
	computes the optimum for problem class $1/P/R = convex/l_2^2/\sum$ and returns the objective value.
double	$P.linf_sum(facilities\& EX)$ computes the optimum for problem class $1/P/./l_{\infty}/\sum$ and returns the objective value.
double	$P.linf_sum(facilities\& EX, restrictions\& R)$
	computes the optimum for problem class $1/P/R = convex/l_{\infty}/\sum$ and returns the objective value.
double	$P.12_sum(facilities\& EX, double epsilon)$
	computes the optimum for problem class $1/P/./l_2/\sum$ (Weiszfeld-Algorithm) and returns the objective value.
double	$P.l2_sum(facilities\& EX, barrier\& R)$
	computes the optimum for problem class $1/P/(R,\infty)/l_2/\sum$ and returns the objective value, where (R,∞) may be one barrier such as a circle, a segment or a polygon.
double	$P.12_sum(facilities\& EX, barrier\& R, bool erase, int choose, double percent, double accel, double init_ss, double epsilon)$
	computes the optimum for problem class $1/P/(R,\infty)/l_2/\sum$ and returns the objective value, where (R,∞) may be one barrier such as a circle, a segment or a polygon. Same algorithm like the above one but user can choose from two heuristics(0 or 1) and define a percentage(percent) of points to handle, acceleration factor(accel) and initial step size(init_ss) as well as epsilon for the iterations.
double	$P.lp_sum(facilities\&\ EX,\ int\ p, double\ epsilon, double\ delta, int\ iter_max)$
	computes the optimum for problem

computes the optimum for problem class $1/P/./l_p/\sum$ (Generalized Weiszfeld-Algorithm) and returns the objective value.

double	$P.lp_sum(facilities\& EX, restrictions\& R, int p, double epsilon, double delta, int iter_max)$	
		computes the optimum for problem class $1/P/R/l_p/\sum$ and returns the objective value.
double	$P.l2sqr_qsum(facilities\& E$	X)
		computes the optimum for problem class $1/P/./l_2^2/Q - \sum$ (Q-criterial problem) and returns the objective value.
double	$P.ll_2sum(facilities\& EX)$	
		computes the optimum for problem class $1/P/./l_1/2 - \sum$ (bi-criterial problem) and returns the objective value.
double	$P.linf_2sum(facilities\& EX)$	-)
		computes the optimum for problem class $1/P/./linf/2 - \sum$ (bi-criterial problem) and returns the objective value.
double	$P.N_1_sum(facilities\& EX$, int n, matrix w)
		computes the optimum for problem class $N/P/./l_1/\sum$ and returns the objective value.
double	$P.N_linf_sum(facilities\& E)$	X, int n, matrix & w)
		computes the optimum for problem class $N/P/./l_{\infty}/\sum$ and returns the objective value.
double	$P.N l2sqr_sum(facilities\& J)$	EX, int n, matrix & w)
		computes the optimum for problem class $N/P/./l_2^2/\sum$ and returns the objective value.
double	$P.N l2sqr_sum(facilities\& J)$	EX, int n, matrix & w)
		computes the optimum for problem class $N/P/./l_p/\sum$ (Version 1) and returns the objective value.
double	$P.N_{12}sqr_sum(facilities\& I)$	EX, int n, matrix & w)
		computes the optimum for problem class $N/P/./l_p/\sum$ (Version 2) and returns the objective value.

102	CHAPTER	R 14. USER INTERFACE CLASS TO LOLA
double	P.L_l2_sum_M3(facilities &I	EX)
		computes the optimum for problem class $1L/P/./l_2/\sum$ and returns the objective value.
double	P.L_l1_sum_M3(facilities & I	$\mathbb{E}X)$
		computes the optimum for problem class $1L/P/./l_1/\sum$ and returns the objective value.
double	$P.L_linf_sum_M3(facilities \&$	zEX)
		computes the optimum for problem class $1L/P/./l_{\infty}/\sum$ and returns the objective value.
double	$P.L_lp_sum_M3(facilities \& I$	EX, int p)
		computes the optimum for problem class $1L/P/./l_p/\sum$ and returns the objective value.
double	$P.L_{l2_sum_M2logM}(facilitie)$	$es \ \&EX)$
		computes the optimum for problem class $1L/P/./l_2/\sum$ with $O(M^2 log M)$ and returns the objective value.
double	P.L_l2_sum_M2(facilities & I	$\mathbb{Z}X)$
		computes the optimum for problem class $1L/P/v_i = 1/l_2 / \sum$ with $O(M^2)$ and returns the objective value.
double	P.L_RkonvPoly_12_sum(facila	ities & EX , restrictions & R)
		computes the optimum for problem class $1L/P/R = convex/l_2/\sum$ and returns the objective value.
double	$P.L_RkonvPoly_lp_sum(facile)$	$ities \& EX, \ restrictions \& R, \ int \ p)$
		computes the optimum for problem class $1L/P/R = convex/l_p/\sum$ and returns the objective value.
double	$P.L_RkonvPoly_l1_sum(facile)$	ities & EX , restrictions & R)
		computes the optimum for problem class $1L/P/R = convex/l_1/\sum$ and returns the objective value.

double	$P.L_RkonvPoly_linf_sum(fa)$	$cilities\& \ EX, \ restrictions\& \ R)$
		computes the optimum for problem class $1L/P/R = convex/l_{inf}/\sum$ and returns the objective value.
double	$P.L_{RkonvPoly_block_sum(j)}$	facilities & EX, restrictions & R, Blocknorm & B)
		computes the optimum for problem class $1L/P/R = convex/l_{block}/\sum$ and returns the objective value.
3.1.2 Cente	r-problems	
double	$P.l1_max(facilities\& EX)$	
		computes the optimum for problem class $1/P/./l_1/max$ and returns the objective value.
double	$P.l1_max(facilities\& EX,$	restrictions & R)
		computes the optimum for problem class $1/P/R = convex/l_1/max$ and returns the objective value.
double	$P.l1_v1_max(facilities\&~EZ)$	X)
		computes the optimum for problem class $1/P/v_i = 1/l_1/max$ and returns the objective value.

double $P.l2_max(facilities\& EX)$

computes the optimum for problem class $1/P/./l_2/max$ and returns the objective value.

double $P.l2_max(facilities\& EX, restrictions\& R)$

computes the optimum for problem class $1/P/R = \text{convex polyhedron}, v_i = 1/l_2/max$ and returns the objective value.

double $P.linf_max(facilities\& EX)$

computes the optimum for problem class $1/P/./l_{\infty}/max$ and returns the objective value.

double $P.linf_max(facilities\& EX, restrictions\& R)$

computes the optimum for problem class $1/P/R = convex/l_{\infty}/max$ and returns the objective value.

double	P.linf_v1_max(facilities& E	CX)
		computes the optimum for problem class $1/P/v_i = 1/l_{\infty}/max$ and returns the objective value.
double	P.elzhearn(facilities& EX)	
		computes the optimum for Elzinga-Hearn- Algorithm and returns the objective value.
double	$P.N_linf_max(facilities\& E$	X, int N, matrix & W)
		computes the optimum for problem class $N/P/./l_{\infty}/max$ and returns the objective value.
double	$P.N_11_max(facilities\& EX$	T, int N, matrix & W)
		computes the optimum for problem class $N/P/./l_1/max$ and returns the objective value.
double	$P.L_{l2}max_M4(facilities \&$	(EX)
		computes the optimum for problem class $1L/P/./l_2/max$ and returns the objective value.
double	$P.L_{l1_max_M4}(facilities \&$	(EX)
		computes the optimum for problem class $1L/P/./l_1/max$ and returns the objective value.
double	$P.L_linf_max_M4(facilities$	& EX)
		computes the optimum for problem class $N/P/./l_{\infty}/max$ and returns the objective value.
double	$P.L_{l2}_{max}_{Mlog}M(facilitie)$	es & EX)
		computes the optimum for problem class $1L/P/v_i = 1/l_2/max$ with $O(MlogM)$ and returns the objective value.
double	$P.L_l2_max_M2logM(facilit$	$ies \ \&EX)$
		computes the optimum for problem class $1L/P/./l_2/max$ with $O(M^2 log M)$ and returns the objective value.

double $P.L_lp_max_M4(facilities \&EX, int p)$

computes the optimum for problem class $1L/P/./l_p/max$ and returns the objective value.

14.2 Algorithm (lgraphalg)

1. Definition

An instance of the data type *lgraphalg* consists of the algorithms to solve location problems with a network or graph.

2. Creation

lgraphalg GrA; creates a variable GrA of type lgraphalg.

3. Operations

$list < sol_typ >$	$GrA.alg_solution()$	returns the solution for the current problem.
void	GrA.WriteOpt(ostream&~off)	ut)

writes the solution for the current problem.

3.1 Algorithms

double	GrA.inmedian(loladirected&	(G)
		computes the In-Median for problem class $1/G_D/./d(V, V)/\sum$ and returns the objective value.
double	GrA. outmedian (loladirected)	& G)
		computes the Out-Median for problem class $1/G_D/./d(V, V)/\sum$ and returns the objective value.
double	GrA.median(loladirected& G)	$\left(\vec{x} \right)$
		computes the median for problem class $1/G_D/./d(V, V)/\sum$ and returns the objective value.
double	GrA.median (lola undirected &	z U)

		computes the optimum for problem class $1/G/./d(V,V)/\sum$ and returns the objective value.
double	$GrA.abs_inmedian(loladirect)$	ted& G)
		computes the In-Median for problem class $1/G_D/./d(V,G)/\sum$ and returns the objective value.
double	$GrA.abs_outmedian(loladire$	cted& G)
		computes the Out-Median for problem class $1/G_D/./d(V,G)/\sum$ and returns the objective value.
double	$GrA.abs_median(loladirected)$	l& G)
		computes the median for problem class $1/G_D/./d(V,G)/\sum$ and returns the objective value.
double	$GrA.abs_median(lolaundired)$	teted & U)
		computes the optimum for problem class $1/G/./d(V,G)/\sum$ and returns the objective value.
double	GrA.center(lola undirected &	G)
		computes the optimum for problem class $1/G/./d(V,V)/\max$ and returns the objective value.
double	GrA.center(loladirected& G)
		computes the optimum for problem class $1/G_D/./d(V,V)/\max$ and returns the objective value.
double	$GrA.abs_center(lola undirect$	ed& U)
		computes the optimum for problem class $1/G/./d(V,G)/$ max and returns the objective value.
double	$GrA.abs_center(loladirected)$	$(k \ G)$
		computes the optimum for problem class $1/G_D/./d(V,G)/\max$ and returns the objective value.

double	$GrA.loc_tree_median(lolatre$	e& U)
		computes the optimum for problem class $1/T/./d(V, V)/\sum$ and returns the objective value.
double	$GrA.abs_tree_median(lolatree)$	ee& U)
		computes the optimum for problem class $1/T/./d(V,T)/\sum$ and returns the objective value.
double	$GrA.loc_tree_center(lolatree)$	& U)
		computes the optimum for problem class $1/T/./d(V, V)/\max$ and returns the objective value.
double	$GrA.abs_tree_center(lolatree)$	& U)
		computes the optimum for problem class $1/T/./d(V,T)/\max$ and returns the objective value.
double	$GrA.tree_two_center(lolatree)$	e& U)
		computes the optimum for problem class $2/T/./d(V,T)/\max$ and returns the objective value.
double	$GrA.N_median_cplex(lolaund)$	directed& U, int n, list <int>& belongto)</int>
		computes the optimum for problem class $N/G/./d(V,V)/\sum$ using cplex and returns the objective value.
double	$GrA.N_median_partitioning($	$lola undirected \&\ U, int\ n, list < int > \&\ belong to)$
		computes the optimum for problem class $N/G/./d(V,V)/\sum$ using the node- partitioning-heuristic and returns the ob- jective value, in the list 'belongto' the membership-information for every node is contained.
double	$GrA.N_median_exchange(lological)$	aundirected & U, int n, list < int > & belong to)
		computes the optimum for problem class $N/G/./d(V,V)/\sum$ using the exchange- heuristic and returns the objective value, in the list 'belongto' the membership- information for every node is contained.

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double	$GrA.N_median_greedy(lolaundirected\&~U, int~n, list < int > \&~belong to)$
	computes the optimum for problem class $N/G/./d(V, V)/\sum$ using the greedy-heuristic and returns the objective value, in the list 'be-longto' the membership-information for every node is contained.
double	$GrA. \texttt{N_center_partitioning}(lolaundirected \& U, int n, list < int > \& belong to)$
	computes the optimum for problem class $N/G/./d(V, V)/$ max using the node- partitioning-heuristic and returns the ob- jective value, in the list 'belongto' the membership-information for every node is contained.
double	$GrA.$ N_center_greedy($lolaundirected \& U, int n, list < int > \& belong to$)
	computes the optimum for problem class $N/G/./d(V,V)/\max$ using the greedy- heuristic and returns the objective value, in the list 'belongto' the membership- information for every node is contained.
list < vector >	$GrA.medPareto_bi(lolaundirected\&~U, list < edge_segment>\&~wholesol)$
	computes the optimum for problem class $1/G/./d(V,G)/2 - \sum_{par}$.
list < vector >	$GrA.medPareto_bi(lolaundirected\&~U, list < edge_segment>\&~wholesol)$
	computes the optimum for problem class $1/G/./d(V,G)/Q - \sum_{par}$.
list < vector >	$GrA.medPareto_bi(lolaundirected\&~U, list < edge_segment>\&~wholesol)$
	computes the optimum for problem class $1/G_D/./d(V,G)/Q - \sum_{par}$.
list < vector >	$GrA.{\tt medPareto_bi}(lola undirected \&\ U, list {\it edge_segment} > \&\ wholesol)$
	computes the optimum for problem class $1/G_D/./d(V,V)/Q - \sum_{par}$.
list < vector >	$GrA.medPareto_bi(lolaundirected\&~U, list < edge_segment>\&~wholesol)$
	computes the optimum for problem class $1/G/./d(V,V)/Q - \sum_{par}$.

list < vector >	$GrA.medPareto_bi(lolaundirec$	ted& U, list <edge_segment>& wholesol)</edge_segment>
		omputes the optimum for problem class $/G_D/./d(V,V)/Q - \max_{par}$.
list < vector >	$GrA.medPareto_bi(lolaundirec$	$ted \& U, list < edge_segment > \& wholesol)$
		omputes the optimum for problem class $/G/./d(V,V)/Q - \max_{par}$.
list < vector >	$GrA.medPareto_bi(lolaundirec$	$ted \& U, list < edge_segment > \& wholesol)$
		omputes the optimum for problem class $/G_D/./d(V,G)/Q - \max_{par}.$
list < vector >	$GrA.medPareto_bi(lolaundirec$	$ted \& U, list < edge_segment > \& wholesol)$
		omputes the optimum for problem class $/G/./d(V,G)/Q - \sum_{lex}$.
list < vector >	$GrA.medPareto_bi(lolaundirec$	$ted \& U, list < edge_segment > \& wholesol)$
		omputes the optimum for problem class $/G_D/./d(V,G)/Q - \sum_{lex}$.
list < vector >	$GrA.medPareto_bi(lolaundirec$	ted& U, list <edge_segment>& wholesol)</edge_segment>
		omputes the optimum for problem class $/G_D/./d(V,V)/Q - \sum_{lex}$.
list < vector >	$GrA.medPareto_bi(lolaundirec$	ted& U, list <edge_segment>& wholesol)</edge_segment>
		omputes the optimum for problem class $/G/./d(V,V)/Q - \sum_{lex}$.
list < vector >	$GrA.medPareto_bi(lolaundirec$	ted& U, list <edge_segment>& wholesol)</edge_segment>
		omputes the optimum for problem class $/G_D/./d(V,V)/Q - \max_{lex}$.
list < vector >	$GrA.medPareto_bi(lolaundirec$	$ted \& U, list < edge_segment > \& wholesol)$
		omputes the optimum for problem class $/G/./d(V,V)/Q - \max_{lex}$.

14.3 Algorithm (gaugealg)

1. Definition

An instance of the data type *gaugealg* consists of the algorithm to solve planar location problems with gauges as the distance functions.

2. Creation

gaugealg GA;	creates a	variable	GA	of	type	gaugealg.

3. Operations

list<location> GA.alg_solution() returns the solution for the current problem.

void GA.WriteOpt(ostream& out)

writes the solution for the current problem.

Algorithms

double	GA.sum(list < polygauge > & LG, list < int > & Ln, facilities & EX)
	computes the optimum for problem class $1/P/./\gamma/\sum$ and returns the objective value.
double	$GA.bi_crit_sum(list\&\ LG,\ list\&\ Ln,\ facilities\&\ EX)$
	computes the optimum for problem class $1/P/./\gamma/2 - \sum_{par}$ and returns the number of different situations of the solution.
double	$GA. \verb"L-block_sum_M3(list < polygauge > \&LG, list < int > \&Ln, facilities \&Ex)$
	$1L/P/./\gamma_B/\sum ext{ with } O(M^3).$
double	$GA.L_block_max_M4(list < polygauge > \&LG, list < int > \&Ln, facilities \&Ex)$
	$1L/P/./\gamma_B/\max ext{ with }O(M^4).$
double	$GA.L_RkonvPoly_block_sum(list \&LG, list \&Ln, facilities EX, restrictions &Restr)$
	$1L/P/./\gamma_B/\max \text{ with } O(M^4).$

LOLA Error Messages

The LOLA specific error messages are numbers of 4 digits (XYZZ). Each digit has a special meaning.

- X identifies the general problem class in which the function that was called is included.
- ${\bf Y}$ identifies the class in which the function that was called is included.
- **ZZ** identifies the function in which the error occurred.

Here we give a table of all currently used error numbers.

Х	Y	ZZ	error in
1	Υ	ZZ	LOLA planar library
2	Υ	ZZ	LOLA graph library
3	Υ	ZZ	LOLA discrete library
1	0	ZZ	LOLA frontend
1	1	ZZ	class loc_vector
1	2	ZZ	class location
1	3	ZZ	class facilities
1	4	ZZ	restrictions
1	5	ZZ	class facs_util
1	6	ZZ	$gauge_util$
1	7	ZZ	gauges
1	8	ZZ	barriers
2	0	ZZ	class lolagraph
2	1	ZZ	$class graph_util$
2	2	ZZ	class lolatree
3	1	ZZ	discrete

In the following each error code will be specified in detail.

Х	Y	ZZ	error in
1	0	01	_algoch ()
1	0	02 - 12	main ()
1	1	01	locvector :: rotate ()
1	2	01	location :: norm ()
		02	location :: $r_angle()$
		03	location :: loc2point ()
		04	location :: $loc2vector$ ()
		05	location :: test_coords ()
		06	location :: test_weights ()
		$07,\!08$	location :: operator[]
		09,10	location :: operator()
		11	location :: operator/
		12	location :: WriteAsPolygonList
1	3	$01,\!02$	facilities :: $n_{median_objective}$ ()
		03	$facilities :: median_objective ()$
		04	facilities :: WriteOpt ()
		05	facilities :: remove ()
		06	facilities :: N_psum ()
		07	facilities :: $linf_v1_max$ ()
		08-30	facilities :: $N_linf_max_mps$ ()
		31 - 33	facilities :: N_11_sum ()
		$34,\!35$	facilities :: refname ()
		36 - 37	facilities :: $N_{linf_{max}}$ ()
		38-41	facilities :: gauge_sum ()
		42-46	facilities :: gauge_bi_crit_sum ()
1	4	01	restr_circle :: restr_circle ()
		02-04	check_simplicity ()
		05	restr_poly :: proj_v1_l2_max ()
		06	retsr_rect :: $proj_v1_l2_max$ ()
		07	restr_rect :: operator[]
		08	restr_rect :: operator()
		09,10	ReadRestr ()
		11	restriction :: $proj_v1_l2_max$ ()
		12	inside_all ()
		13	polygon_barrier :: polygon_barrier ()
		14	polygon_barrier :: polygon_barrier
1	5	01-07	$fac_util :: ReadLoc ()$
		08-11	fac_util :: ReadMat ()
		12	fac_util :: SaveLoc ()
		13	$fac_util :: SaveLoc_Res ()$
		14	fac_util :: View ()
1	6	$01,\!02$	ReadGNumber ()
		03-06	ReadGauge ()
		$07,\!08$	ReadLPGauge ()
	I	09,10	ReadLMGauge ()

		11	ViewGauge ()
1	7	01-03	polygauge :: polygauge ()
		04	polygauge :: scale
		05	polygauge :: operator []
		$06,\!07$	polygauge :: conepoints
		08,09	polygauge :: conepoints polygauge :: coneseg ()
		10, 11	polygauge :: conetest ()
		12	polygauge :: pl_inCone
		13	polygauge :: ll_inCone
		14	polygauge :: maxi
		15	polygauge :: mini
		16	polygauge :: max_diff
		17-21	mixgauge :: mixgauge ()
		22	mixgauge :: operator [] ()
		23	mixgauge :: conetype ()
		$24,\!25$	mixgauge :: conepoints ()
		$26,\!27$	mixgauge :: coneseg ()
		$28,\!29$	mixgauge :: conetest ()
		30	mixgauge :: pl_inCone ()
		31	mixgauge :: ll_inCone ()
		32	mixgauge :: maxi ()
		33	mixgauge :: mini ()
		34	$mixgauge :: max_diff()$
		35	mixgauge :: scale ()
1	8	$01,\!02$	barrier :: $l2_sum$ ()
		03	halfspace :: compute ()
		04	tree :: flow_rank ()
		05	tree :: $crash_rank$ ()
		06	$sbo :: opt_shdw_segments ()$
2	0	01	$lolagraph :: shortest_path ()$
		02	$lolagraph :: inz_edge ()$
		03	lolagraph :: parlocation ()
2	1	01	graph_util :: LGraphView ()
		02	$graph_util :: ReadAdjlist$
		03	$graph_util :: SaveAdjlist ()$
		04	$graph_util :: SaveGraph ()$
		05-12	$graph_util :: ReadGraph ()$
2	2	01	lolatree :: lolatree ()
		02-04	$lolatree :: tree_med ()$
3	1	01	discrete :: UFLP_dualoc ()
		02	discrete :: SaveDisc $()$
		03-05	discrete :: disc_read () $($
		06-07	discrete :: Read_discrete ()

IMPRESSUM

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